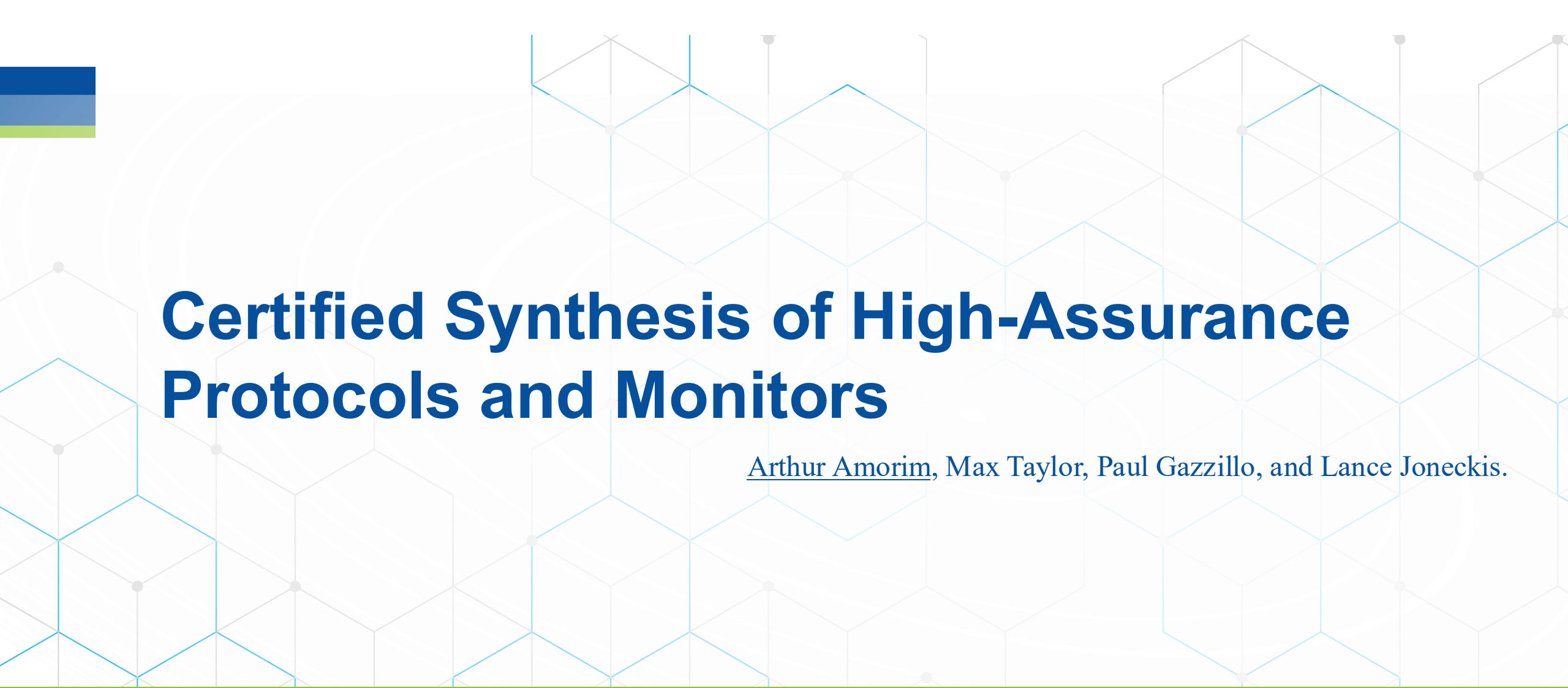




Certified Synthesis of High-Assurance Protocols and Monitors

Arthur Amorim, Max Taylor, Paul Gazzillo, and Lance Joneckis.

One Verified Model, Three
Certified Artifacts

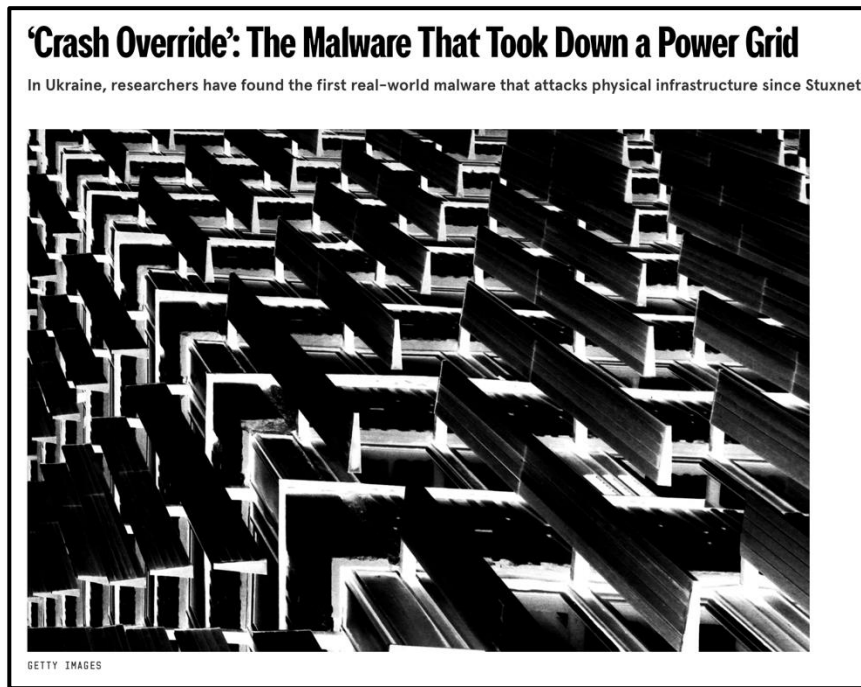


Cyber-Physical Systems Are Now Targets for Physical Damage via Cyber Attacks

Stuxnet



Crash Override



German Steel Mill



Stealthy Attacks Use Only Valid Commands in the Wrong Order

TECH + ENGINEERING

Cyber Attack on German Steel Mill Leads to 'Massive' Real World Damage

A steel mill in Germany lost control of its blast furnace. Hackers had infiltrated the mill's control system, according to the German government's office for information security.

BY R.A. BECKER THURSDAY, JANUARY 8, 2015 NOVA NEXT



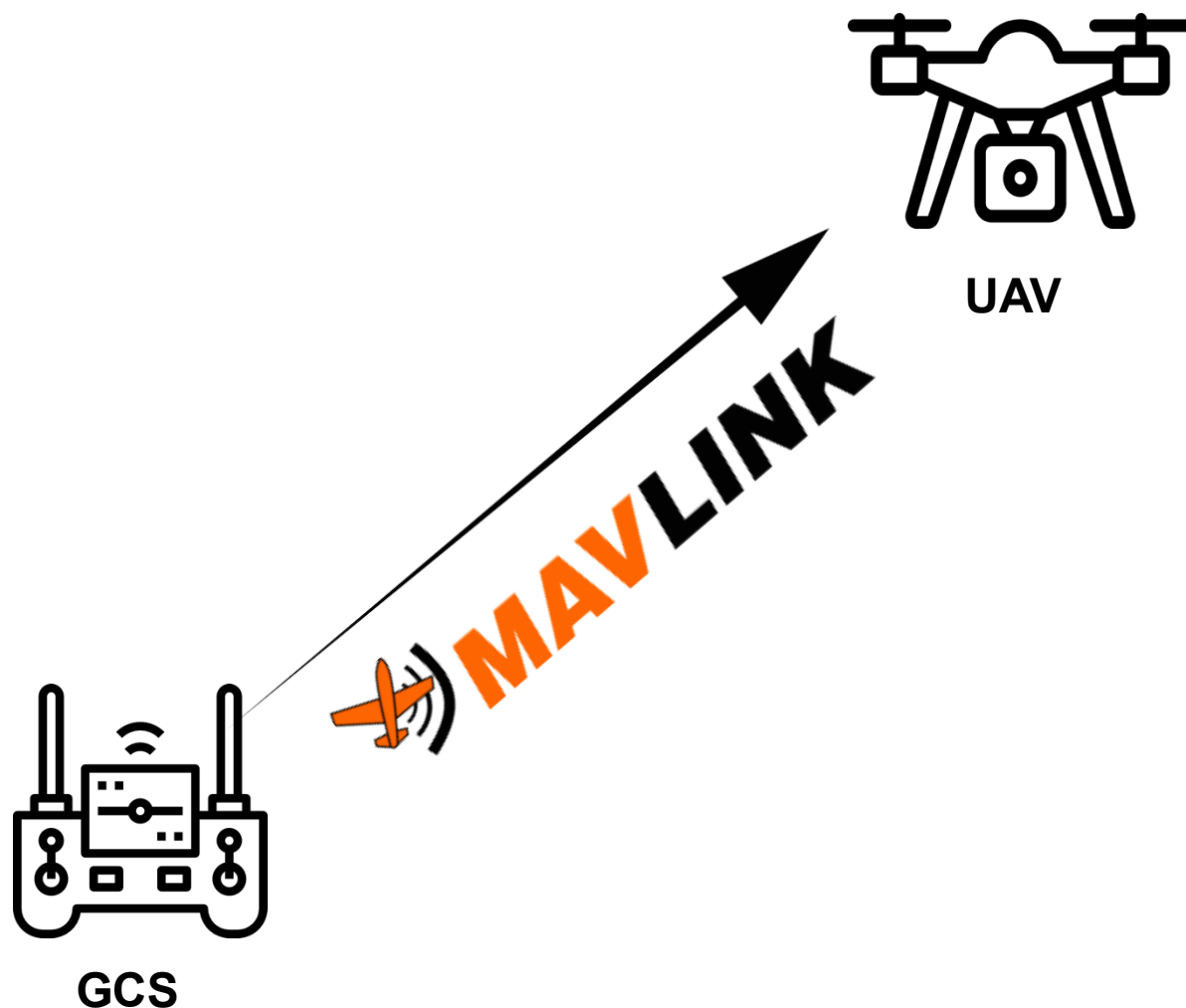
Blasting Furnace Shutdown Sequence:

1 2 3
Reduce_Temp → Release_Pressure → Close_Valves

1 3 2
Reduce_Temp → Close_Valves → Release_Pressure

Stealthy attack: valid commands, wrong order

Widely Used Protocols Are Susceptible to Stealthy Attacks



RVFUZZER: Finding Input Validation Bugs in Robotic Vehicles Through Control-Guided Testing

Taegyu Kim[†], Chung Hwan Kim^{*}, Junghwan Rhee^{*}, Fan Fei[†], Zhan Tu[†], Gregory Walkup[†]

Xiangyu Zhang[†], Xinyan Deng[†], Dongyan Xu[†]

[†]Purdue University, {tgkim, feif, tu17, gwalkup, xyzhang, xdeng, dxu}@purdue.edu

^{*}NEC Laboratories America, {chungkim, rhee}@nec-labs.com

Found 89 input validation bugs

PGFUZZ: Policy-Guided Fuzzing for Robotic Vehicles

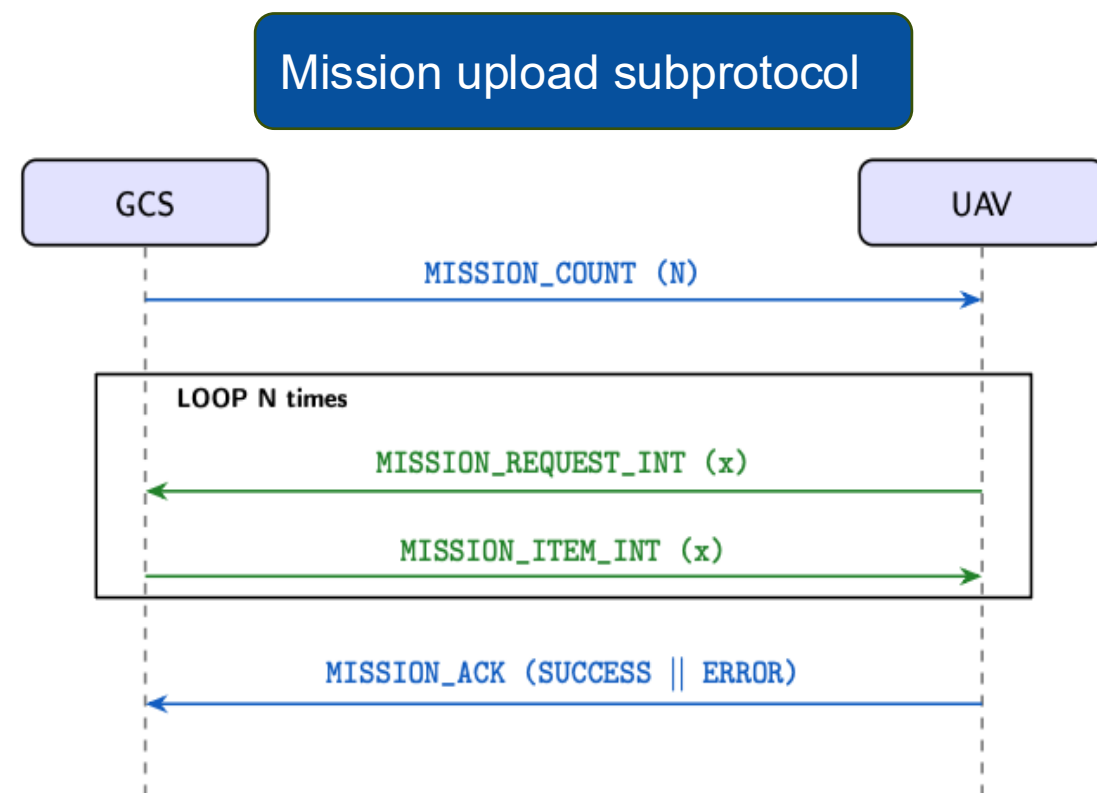
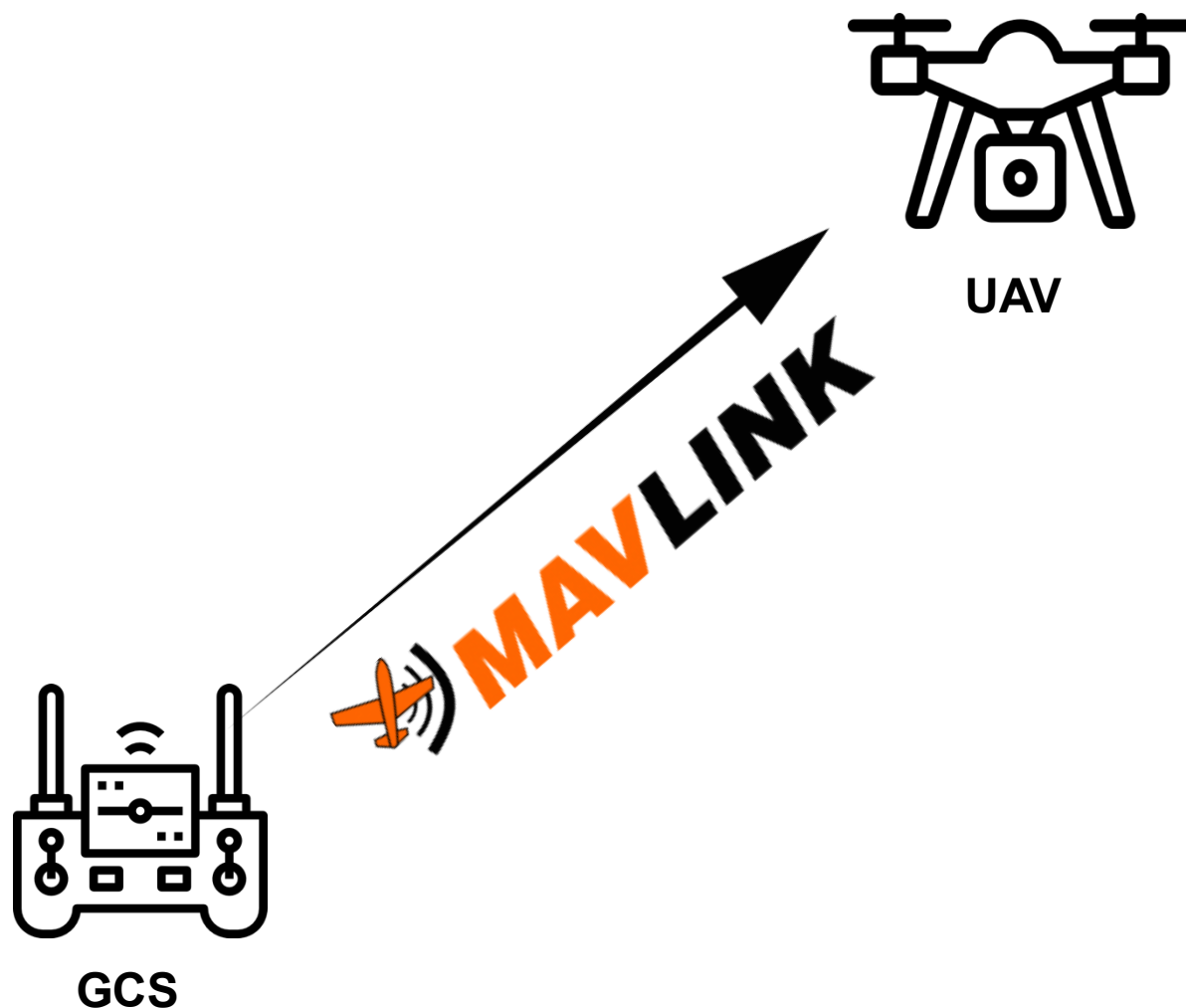
Hyungsub Kim, Muslum Ozgur Ozmen, Antonio Bianchi, Z. Berkay Celik, and Dongyan Xu

Purdue University

{kim2956, mozmen, antoniob, zcelik, dxu}@purdue.edu

Found 156 policy violation bugs

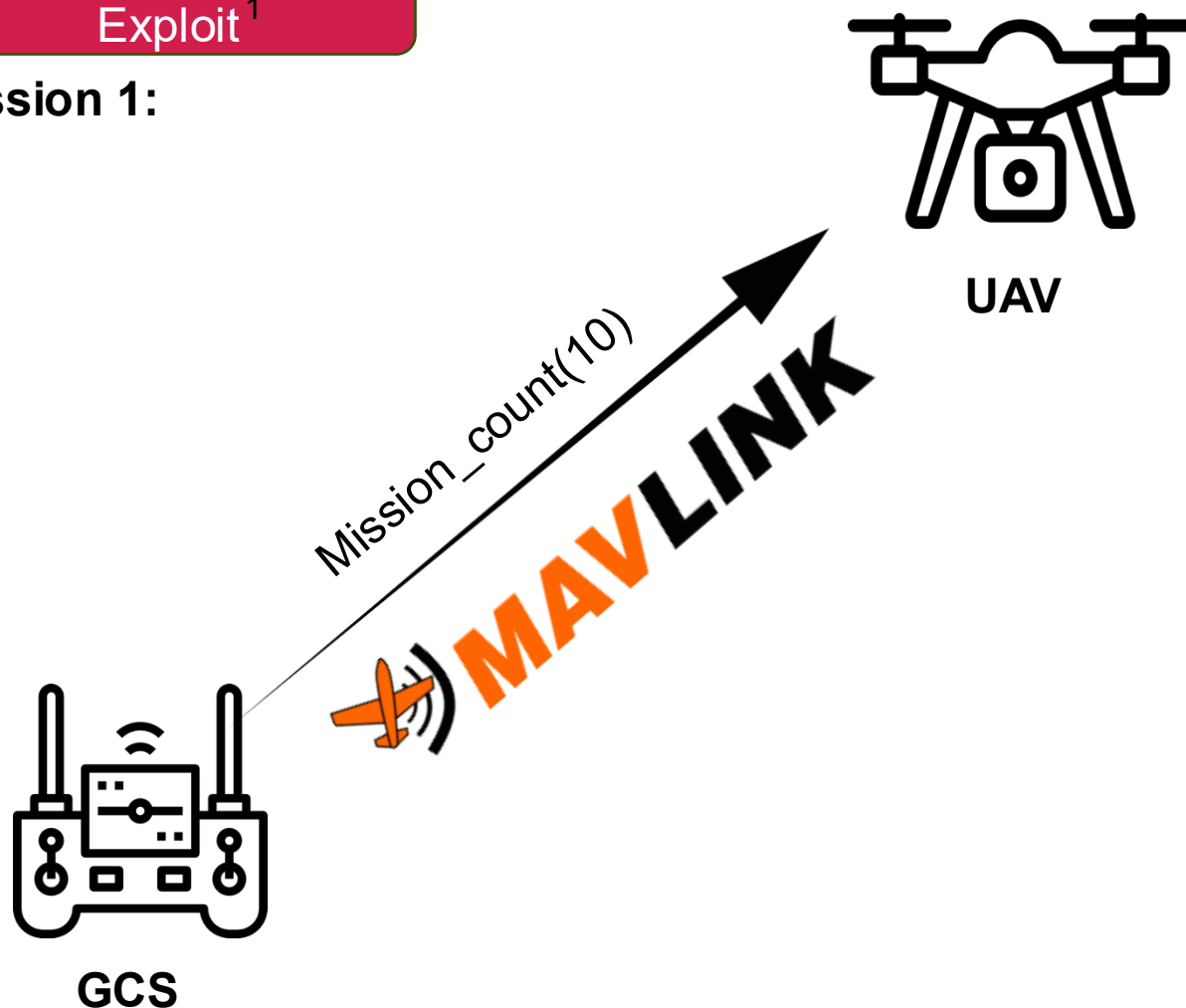
Widely Used Protocols Are Susceptible to Stealthy Attacks



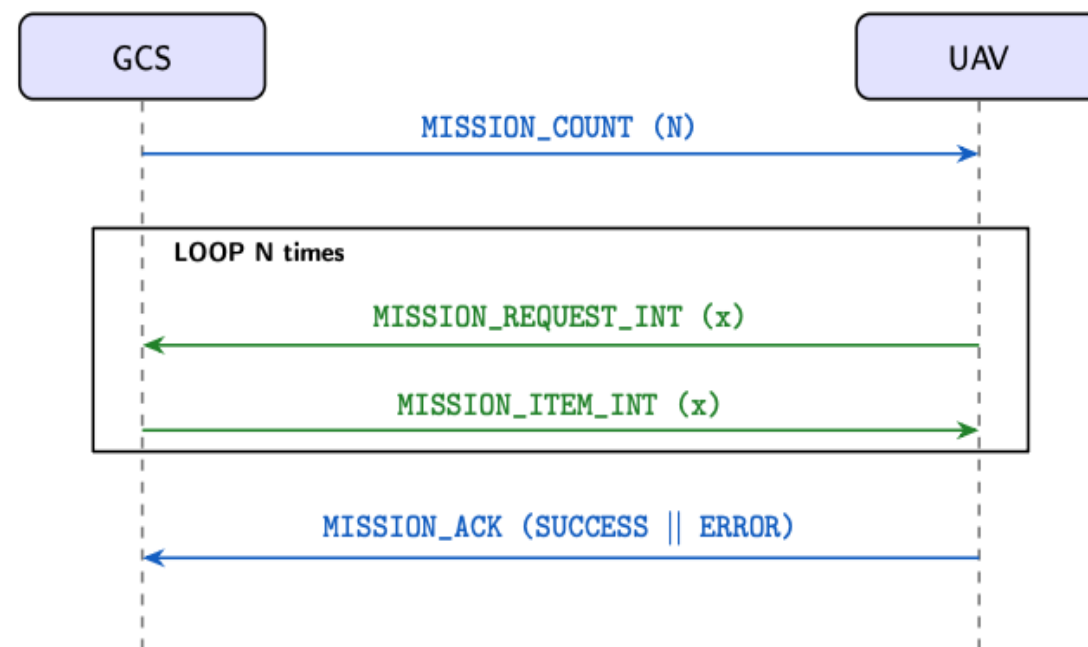
Widely Used Protocols Are Susceptible to Stealthy Attacks

Resource Usage
Exploit¹

Mission 1:



Mission upload subprotocol

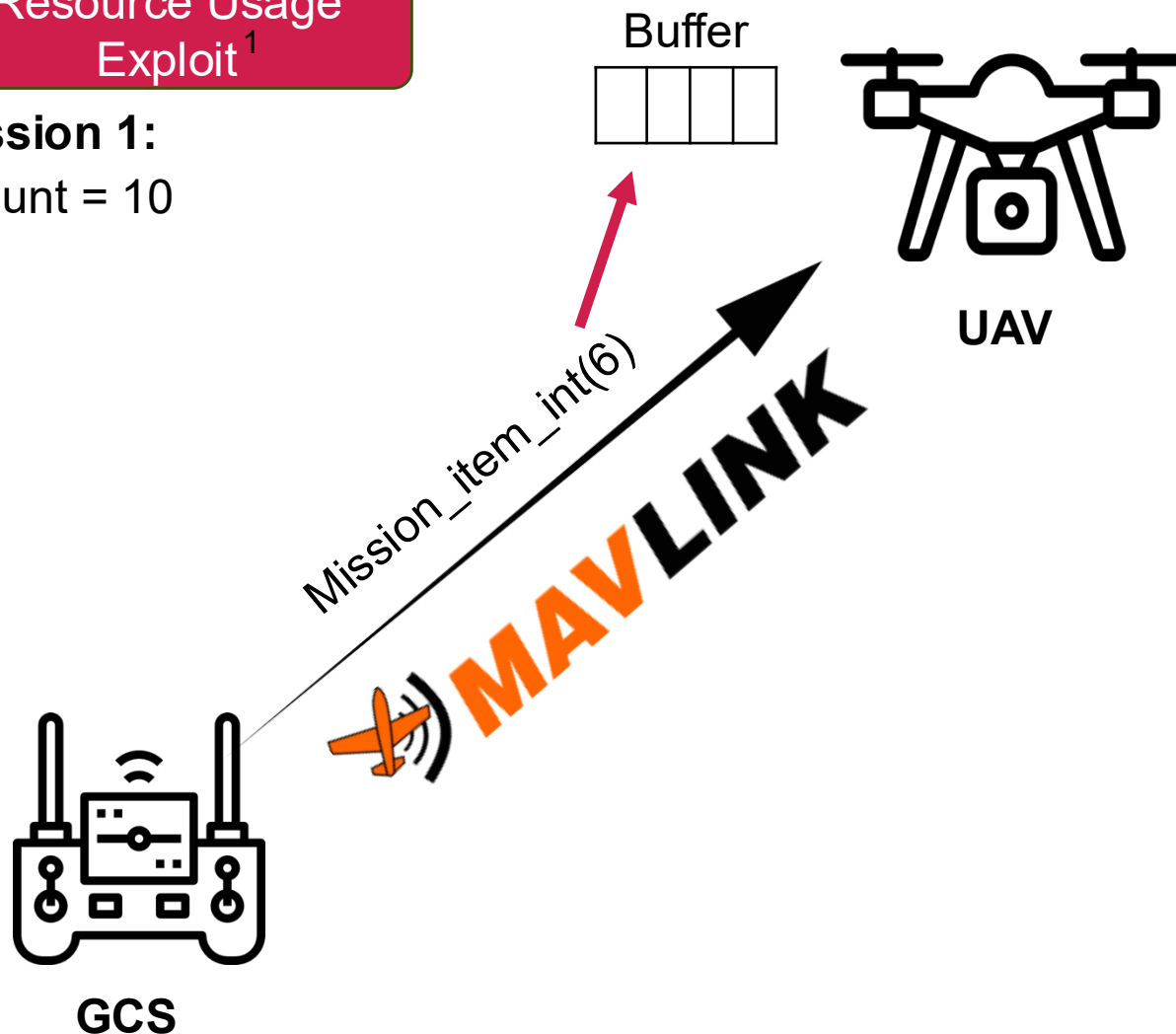


Widely Used Protocols Are Susceptible to Stealthy Attacks

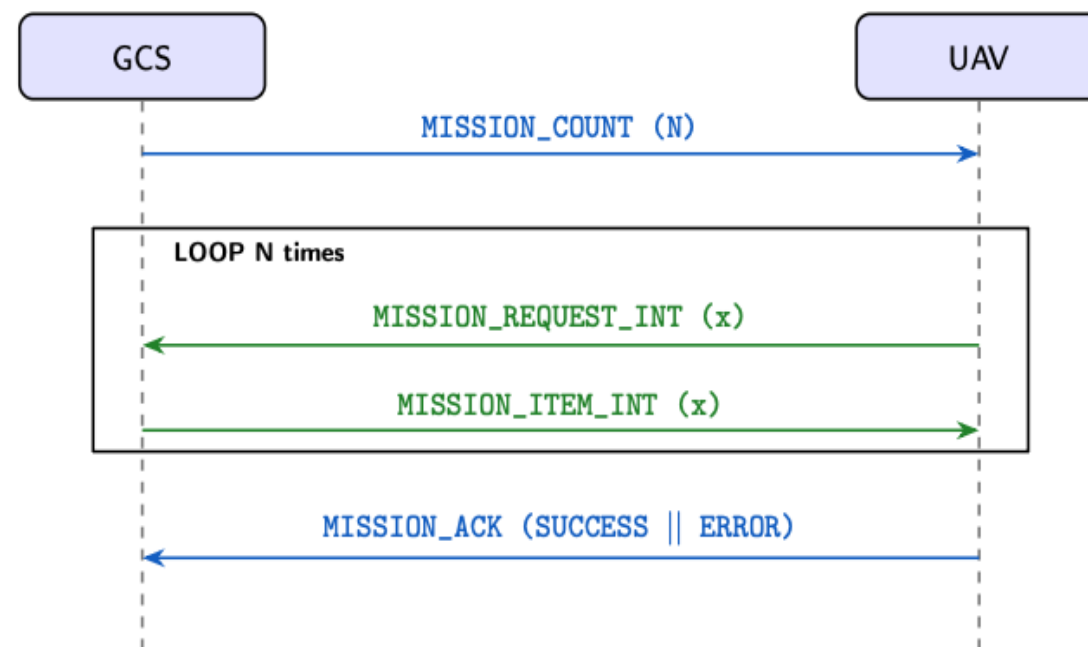
Resource Usage
Exploit¹

Mission 1:

Count = 10



Mission upload subprotocol



Widely Used Protocols Are Susceptible to Stealthy Attacks

Resource Usage
Exploit¹

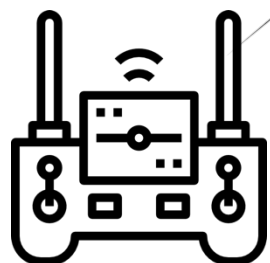
Mission 1:

Count = 10

Buffer
6 7 8 9



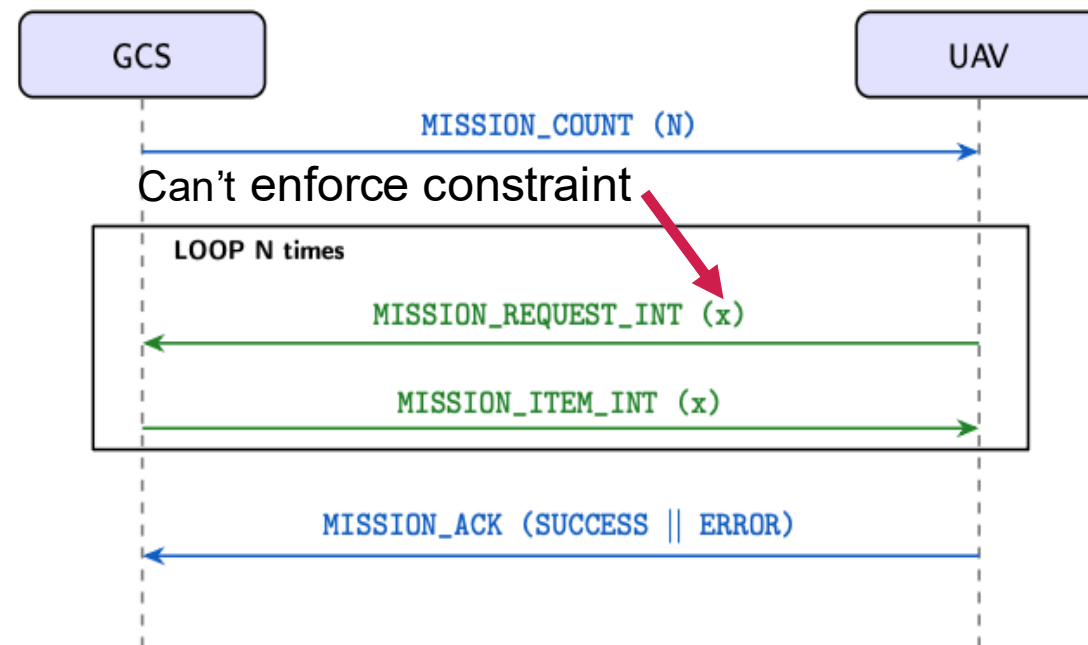
UAV



GCS

Mission_item_int(13)
MAV LINK

Mission upload subprotocol



Widely Used Protocols Are Susceptible to Stealthy Attacks

Resource Usage
Exploit¹

Mission 1:

Count = 10

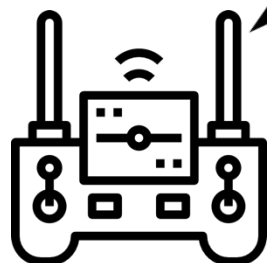
Buffer
6 7 8 9



UAV

Mission_ack(Success)

MAV LINK



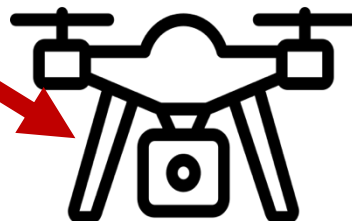
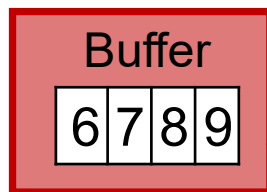
GCS

Widely Used Protocols Are Susceptible to Stealthy Attacks

Resource Usage
Exploit¹

Mission 2:

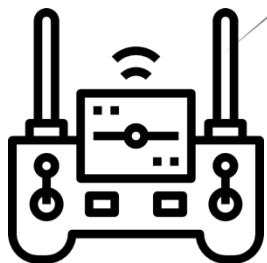
Count = 15



UAV

Mission_item_int(5)

MAV LINK



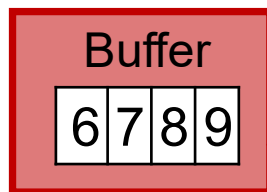
GCS

Widely Used Protocols Are Susceptible to Stealthy Attacks

Resource Usage
Exploit¹

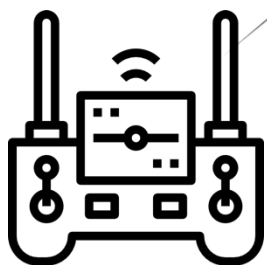
Mission 2:

Count = 15



UAV

UAV starts behaving as mission 1
in the middle of mission 2



GCS

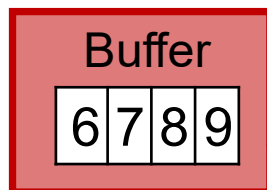


Existing Defenses Miss the Logical Layer

Resource Usage
Exploit¹

Mission 2:

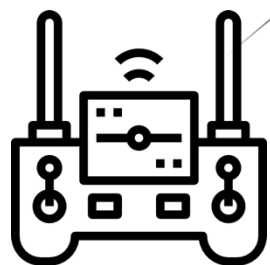
Count = 15



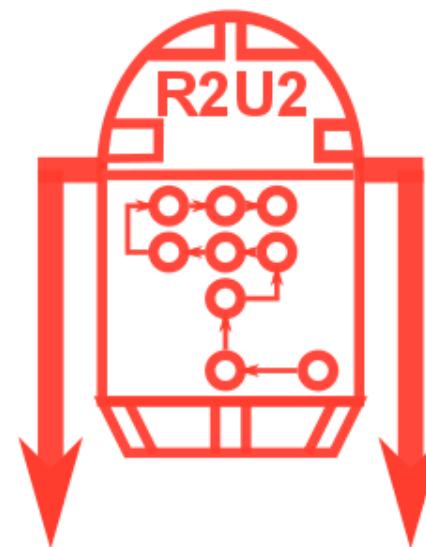
UAV

Problem: A stealthy attack are invisible to approaches that focus on catching bad behavior at runtime

UAV starts behaving as mission 1 in the middle of mission 2



GCS



Intrusion detection systems:
No anomalous behavior or
virus signature

Physics based anomaly
detection: no anomalous
physical deviation.

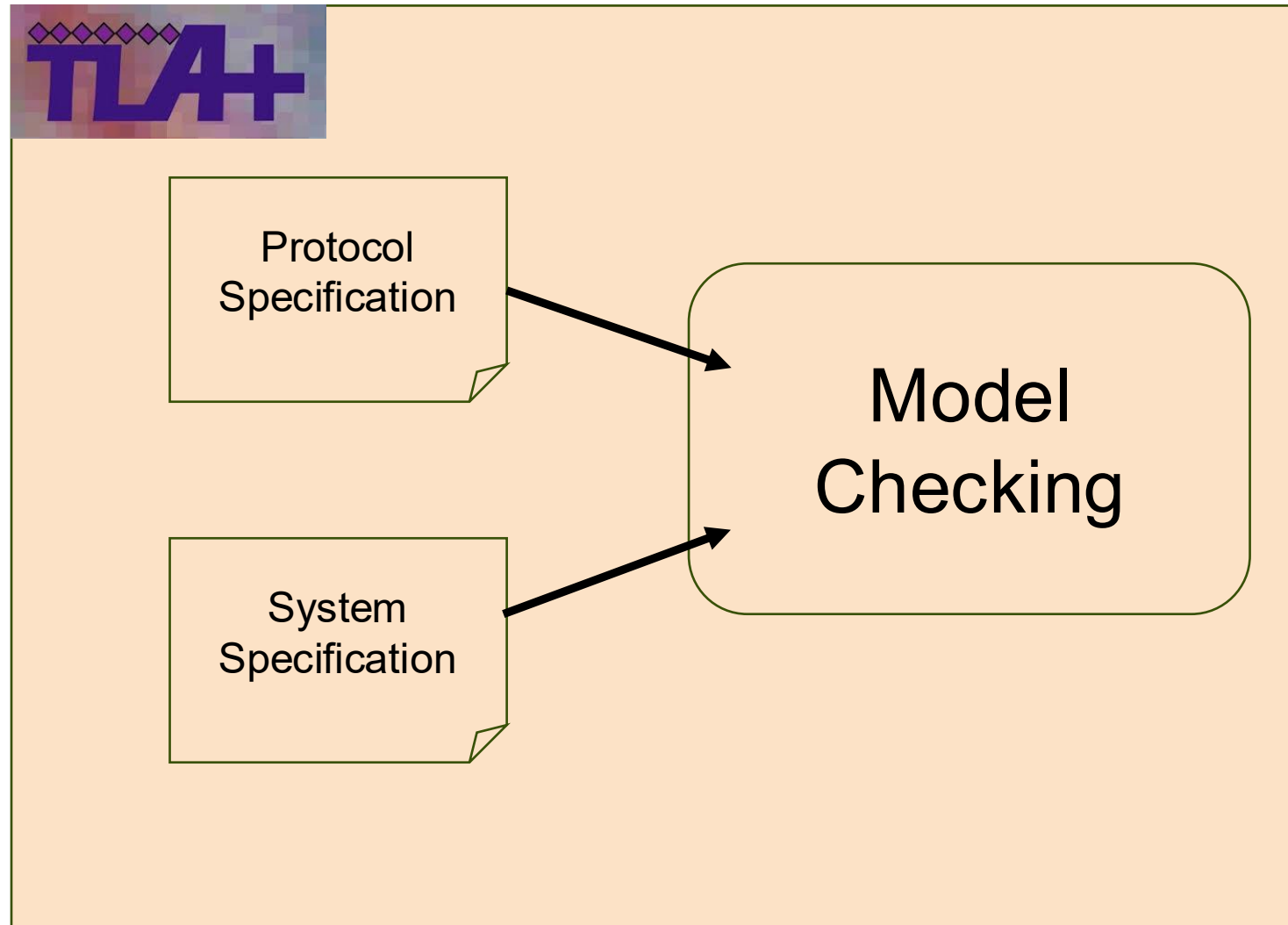


Limitations of Formal Tools

Formal methods prevents unsafe sequences from being represented

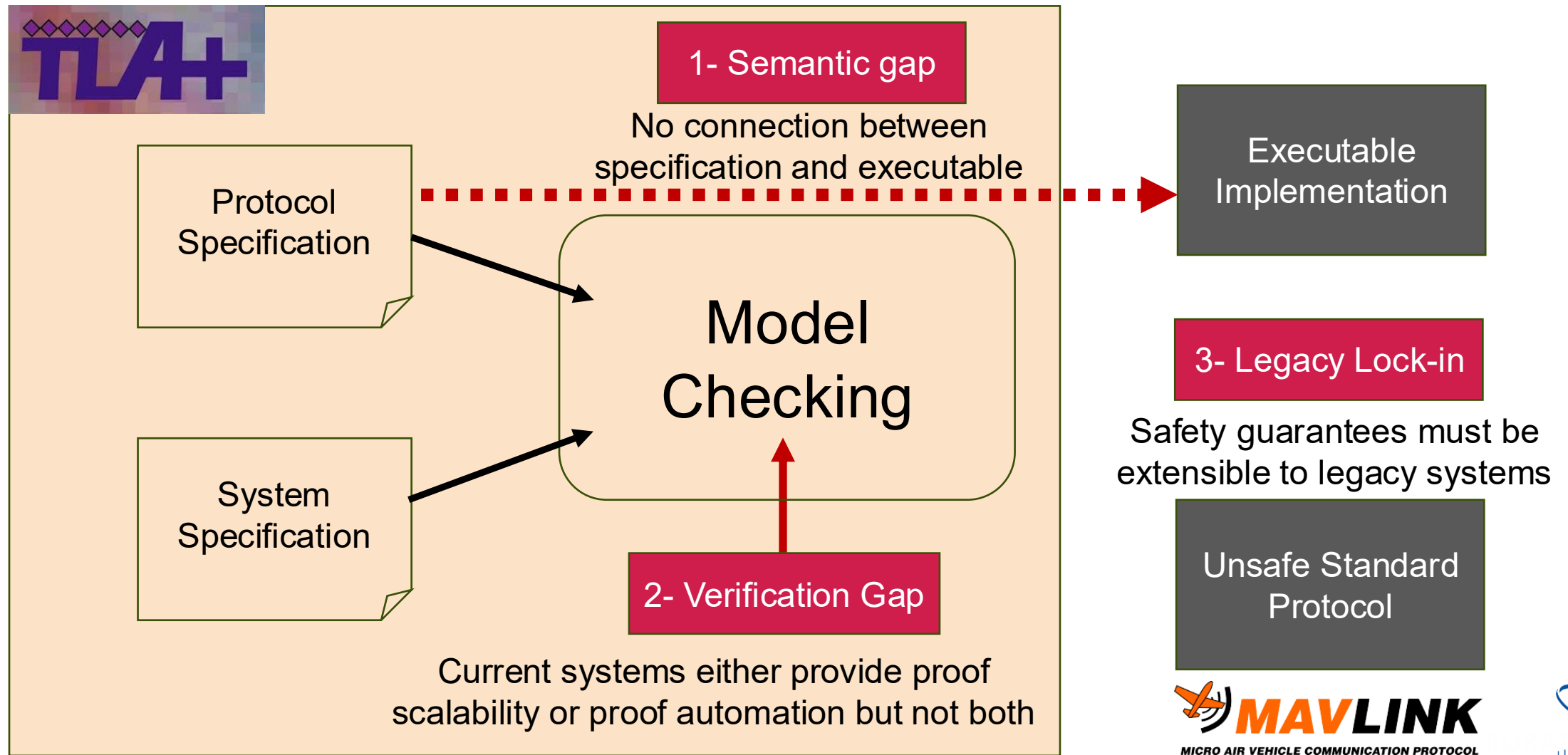
Limitations of Formal Tools

Formal methods prevents unsafe sequences from being represented



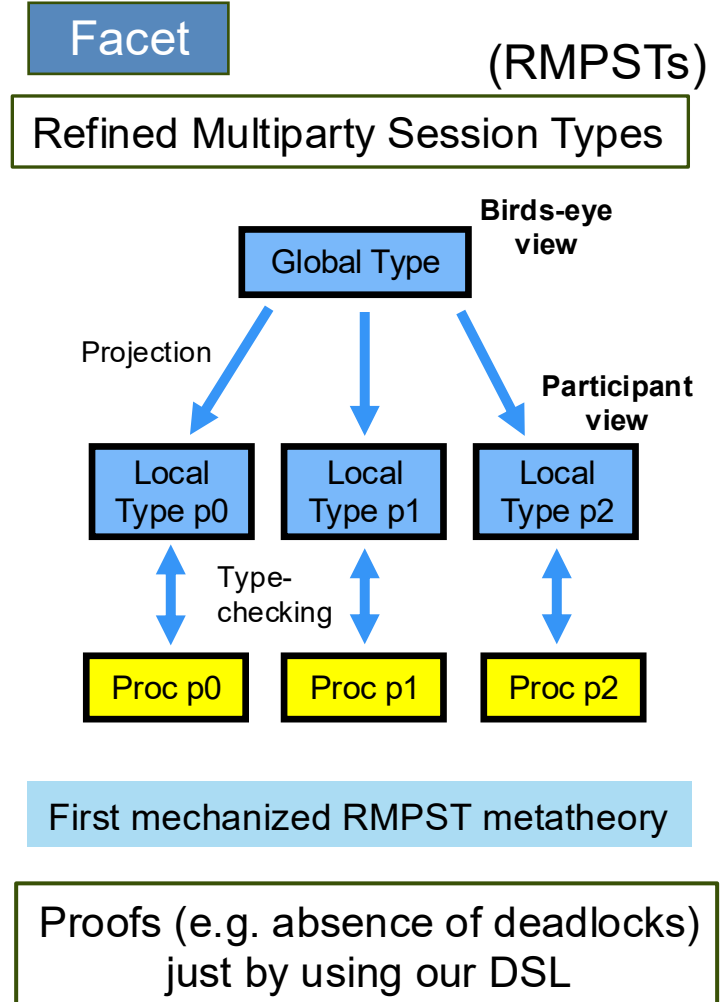
Limitations of Formal Tools

Formal methods prevents unsafe sequences from being represented



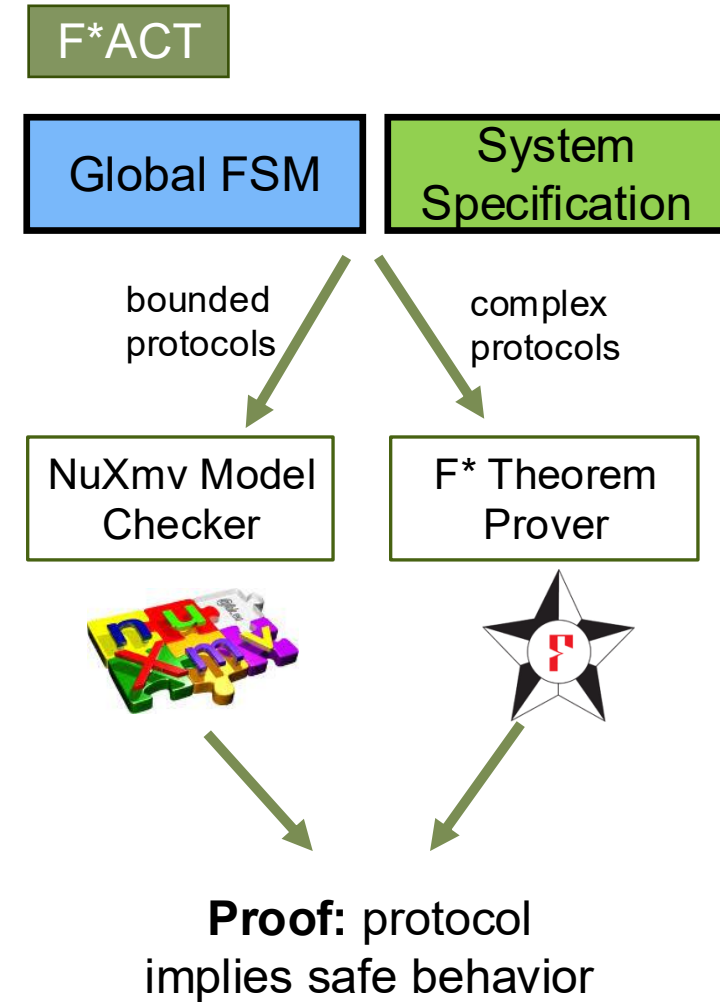
Contributions

1. End-to-end formally verified pipeline from protocol specification to executable code



Contributions

1. End-to-end formally verified pipeline from protocol specification to executable code
2. Dual verification path providing either automatic model checking or theorem-prover pathways.

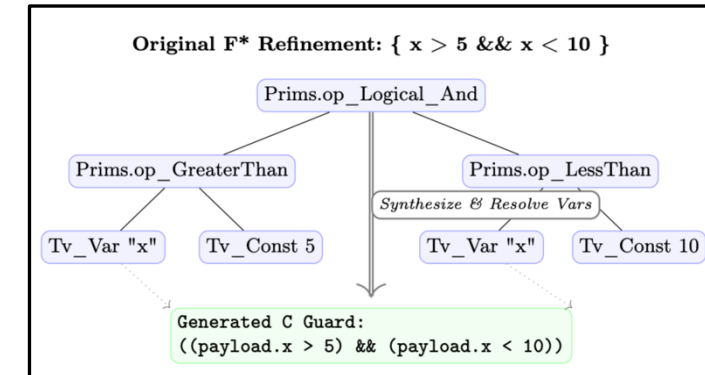


Contributions

1. End-to-end formally verified pipeline from protocol specification to executable code
2. Dual verification path providing either automatic model checking or theorem-prover pathways.
3. Runtime monitors that retrofit legacy protocols with the same level of assurance.

Platum

retrofits existing protocols



Memory overhead: 8.39Mb
Latency overhead: 13.33μs

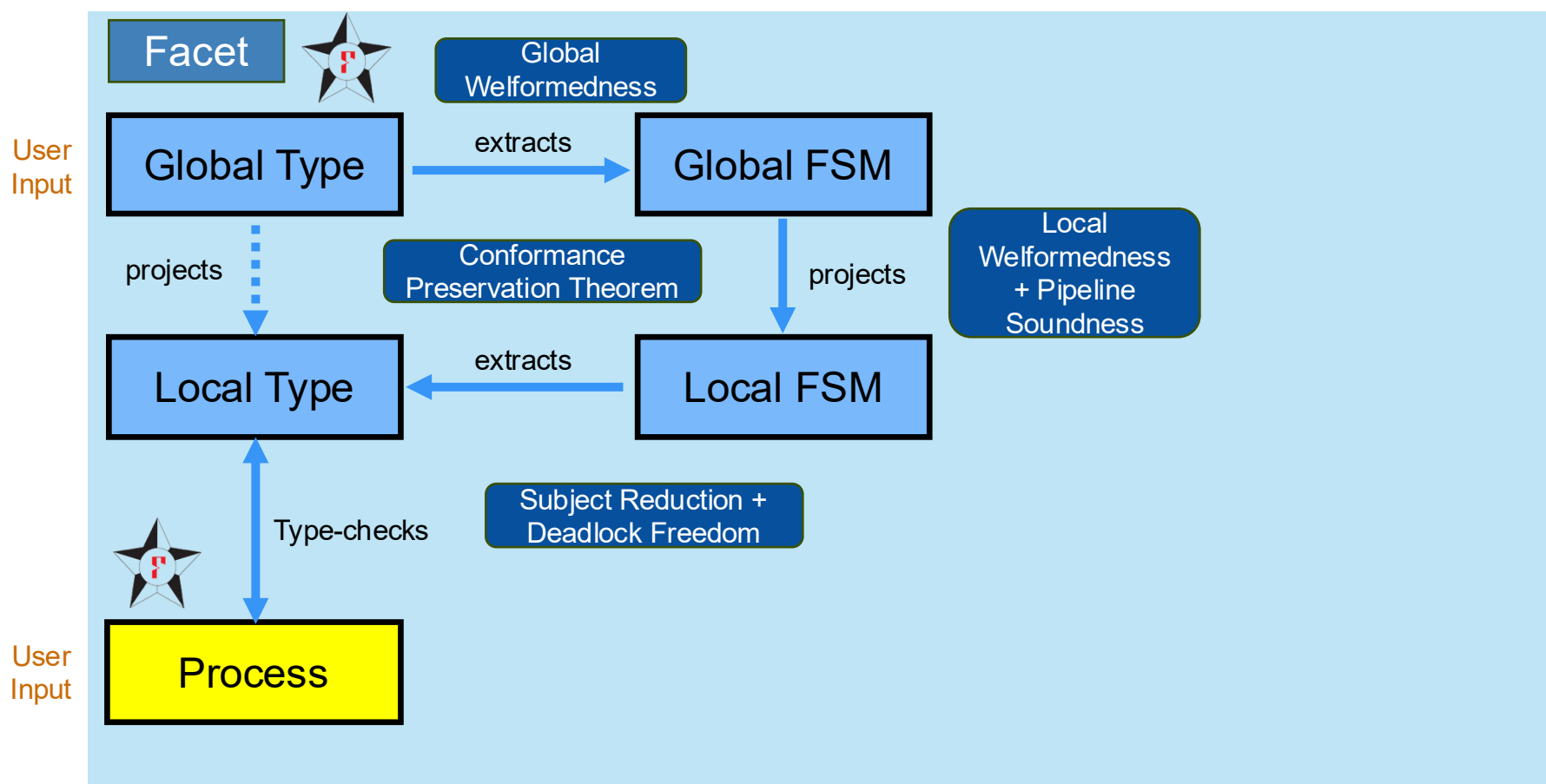


Contributions

1. End-to-end formally verified pipeline from protocol specification to executable code
2. Dual verification path providing either automatic model checking or theorem-prover pathways.
3. Runtime monitors that retrofit legacy protocols with the same level of assurance.
4. Single certified semantic model shared across all generated deployment artifacts

Facet: Mechanized RMPST metatheory in F*

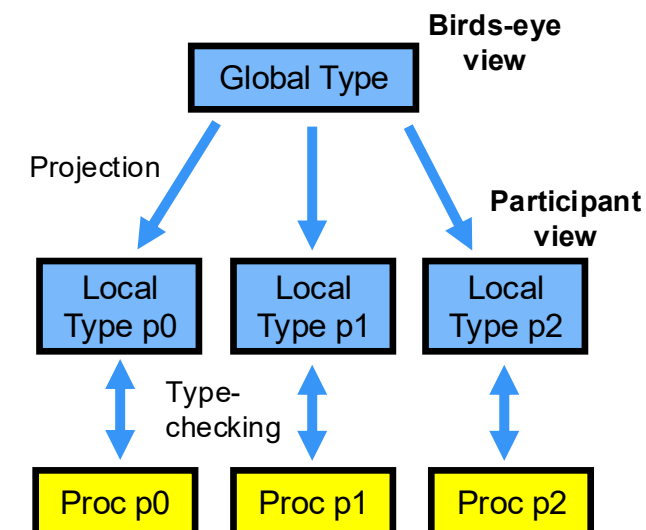
1- Semantic Gap



Facet

(RMPSTs)

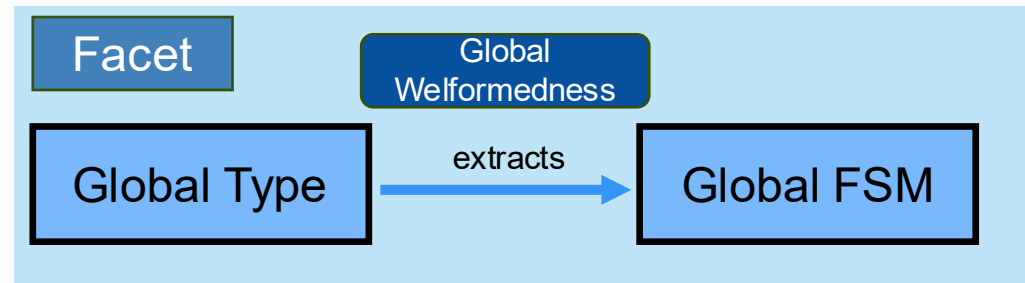
Refined Multiparty Session Types



First mechanized RMPST metatheory

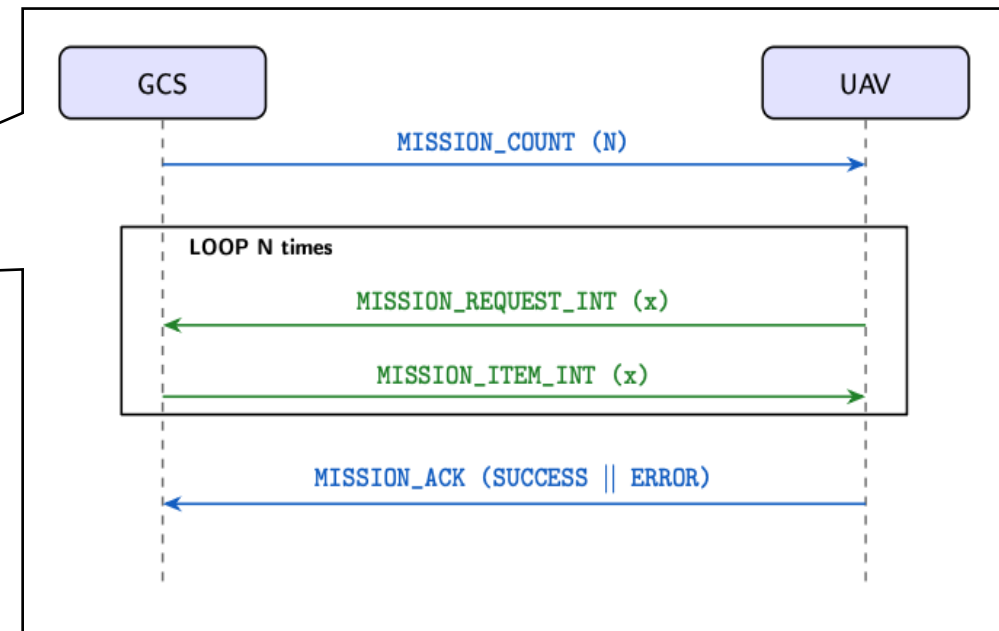
Proofs (e.g. absence of deadlocks)
just by using our DSL

Defining an RMPST for the Mission Upload Protocol.

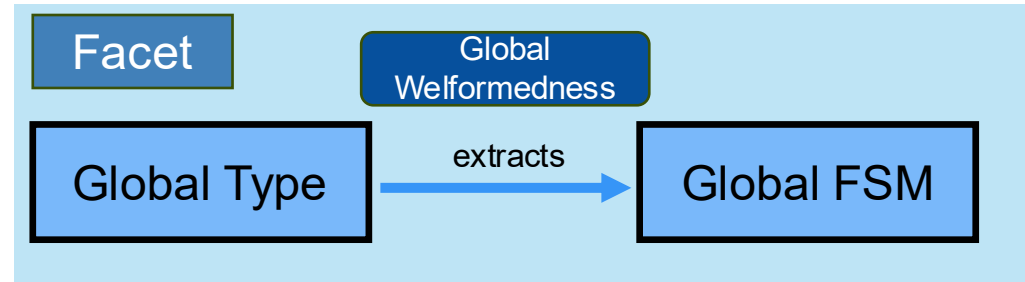


RMPST

```
GCS → UAV: MISSION COUNT( $n\{1 \leq n < \text{LIMIT}\}$ )  
 $\mu.T(\text{curr}\{0 \leq \text{curr} < n\})(\text{curr} = 0)$   
UAV → GCS:  
  MISSION REQUEST INT( $\text{req}\{\text{req} = \text{curr} < n\}$ )  
  MISSION ITEM INT( $\text{item}\{\text{item} = \text{curr} < n\}$ )  
   $T(\text{curr} + 1)$   
 $\oplus$  MISSION ACK( $\text{ack}\{\text{type} = \text{ERROR} \vee \text{curr} = n\}$ ).End
```



Defining an RMPST for the Mission Upload Protocol.



RMPST

GCS $\rightarrow$ UAV: MISSION COUNT($n\{1 \leq n < \text{LIMIT}\}$)

1 $\mu.T(\text{curr}\{0 \leq \text{curr} < n\})(\text{curr} = 0)$

UAV $\rightarrow$ GCS:

MISSION REQUEST INT($\text{req}\{\text{req} = \text{curr} < n\}$)

MISSION ITEM INT($\text{item}\{\text{item} = \text{curr} < n\}$)

$T(\text{curr} + 1)$

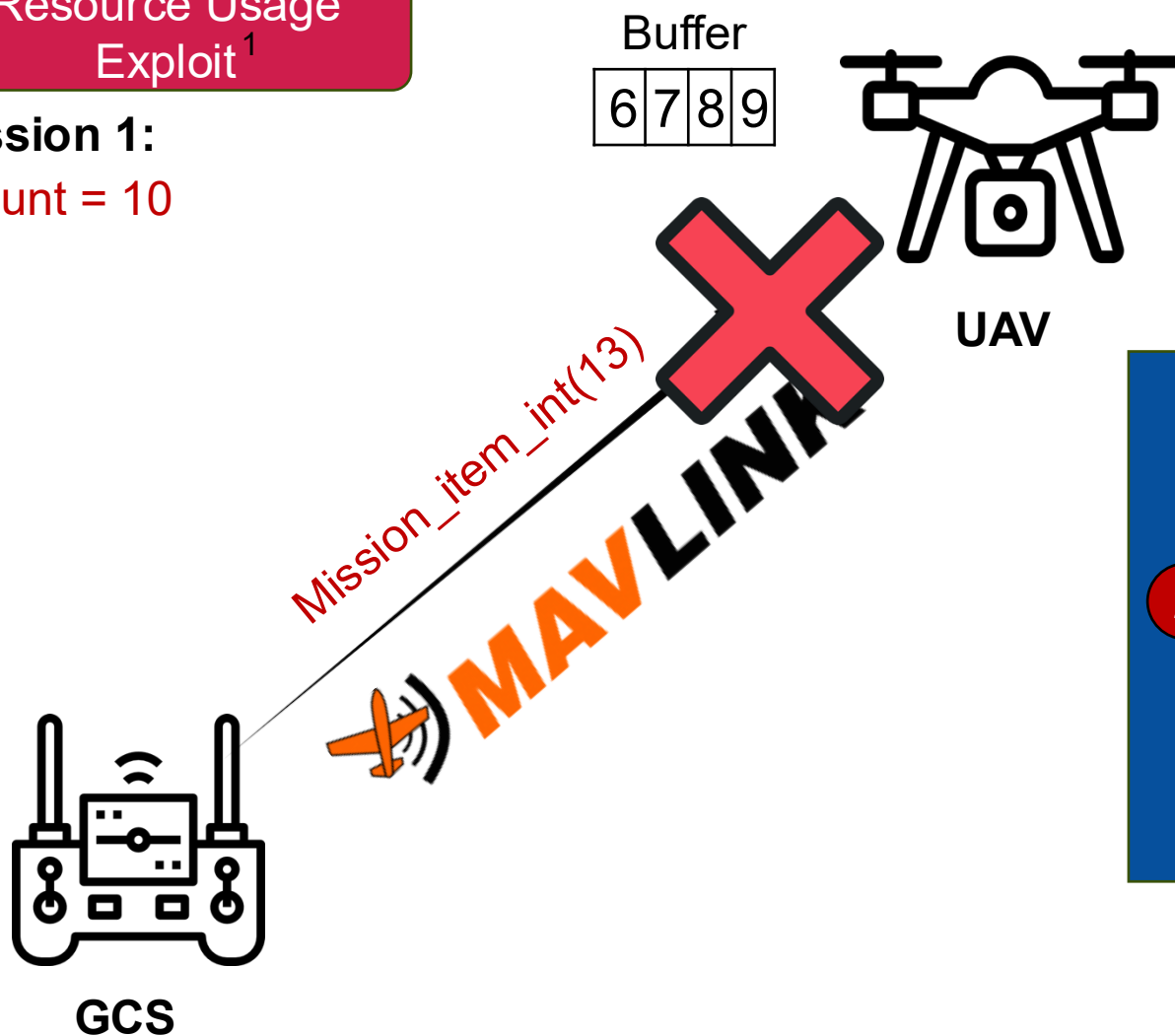
$\oplus$ MISSION ACK($\text{ack}\{\text{type} = \text{ERROR} \vee \text{curr} = n\}$).End

- 1 Create a recursive variable *curr* that must be less than or equal to *n*
- 2 Ensure messages are uploaded in the correct order and not skipped
- 3 The protocol must only complete with *curr* = *n* or with an error message.

Defining an RMPST for the Mission Upload Protocol.

Resource Usage
Exploit¹

Mission 1:
Count = 10



- 2 Ensure messages are uploaded in the correct order and not skipped

Defining an RMPST for the Mission Upload Protocol.

Resource Usage
Exploit¹

Mission 1:
Count = 10

Buffer
6 7 8 9



UAV

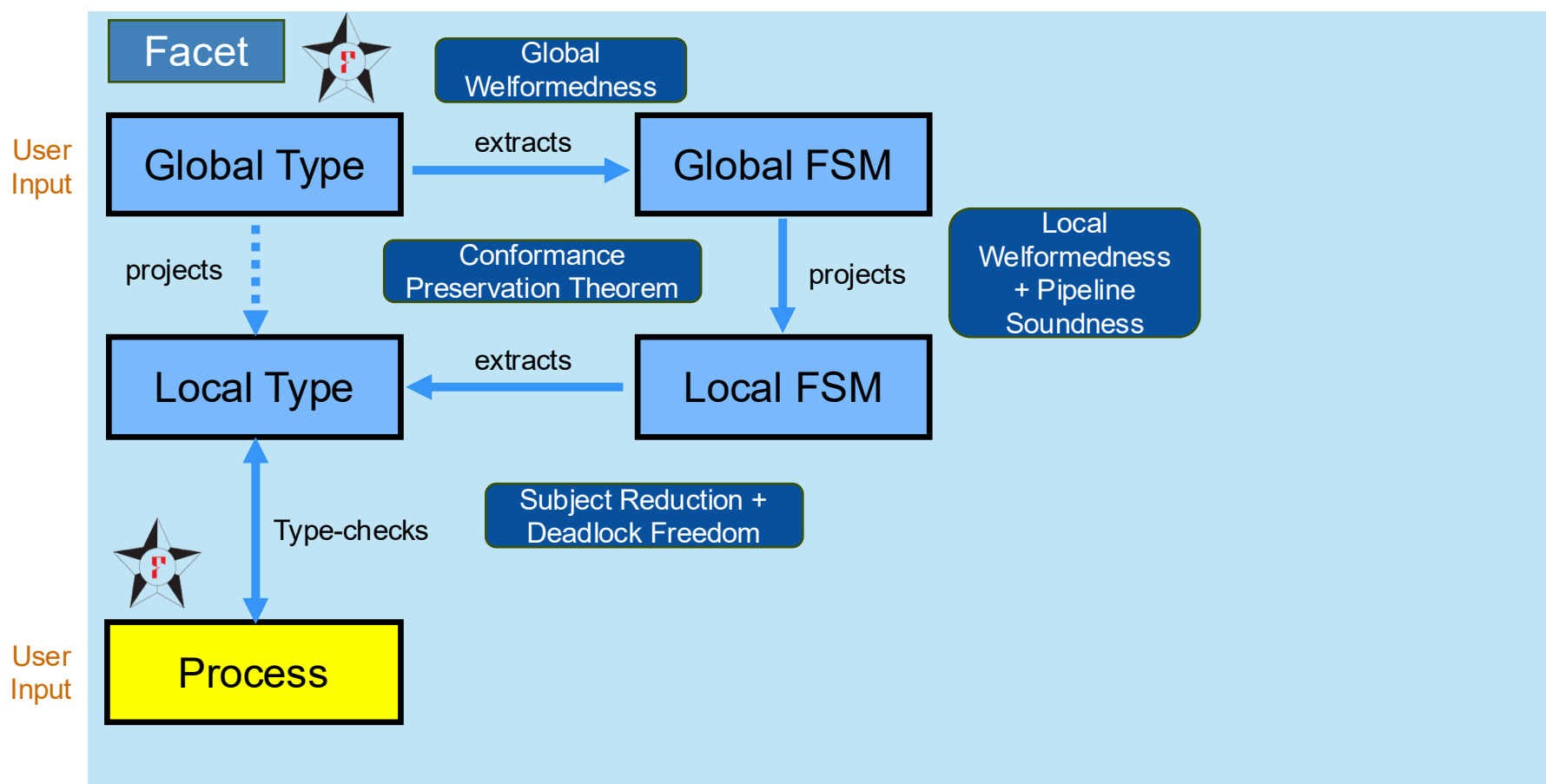


GCS

3 The protocol must only complete with *curr* = *n* or with an error message.

Facet: Mechanized RMPST metatheory in F*

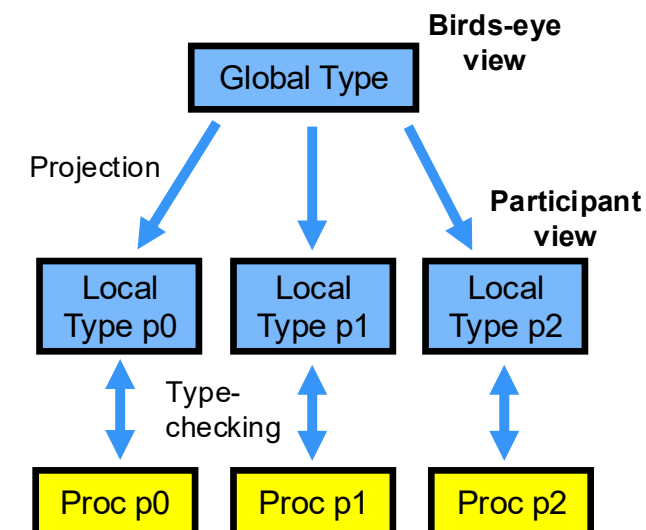
1- Semantic Gap



Facet

(RMPSTs)

Refined Multiparty Session Types

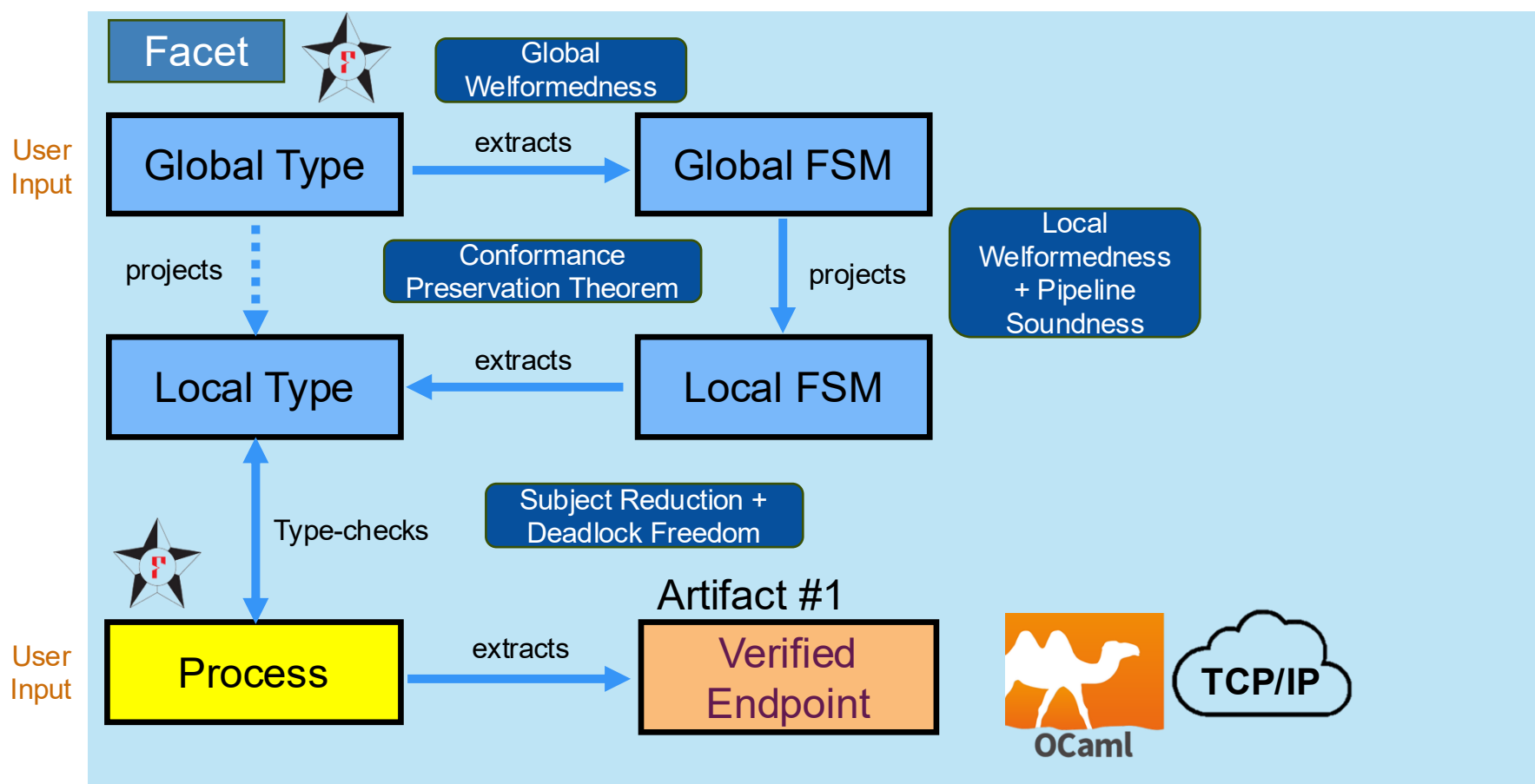


First mechanized RMPST metatheory

Proofs (e.g. absence of deadlocks)
just by using our DSL

Facet: Mechanized RMPST metatheory in F*

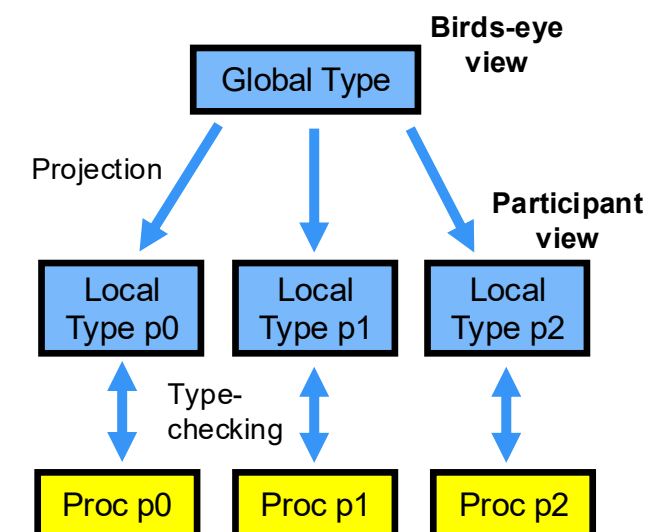
1- Semantic Gap



Facet

(RMPSTs)

Refined Multiparty Session Types

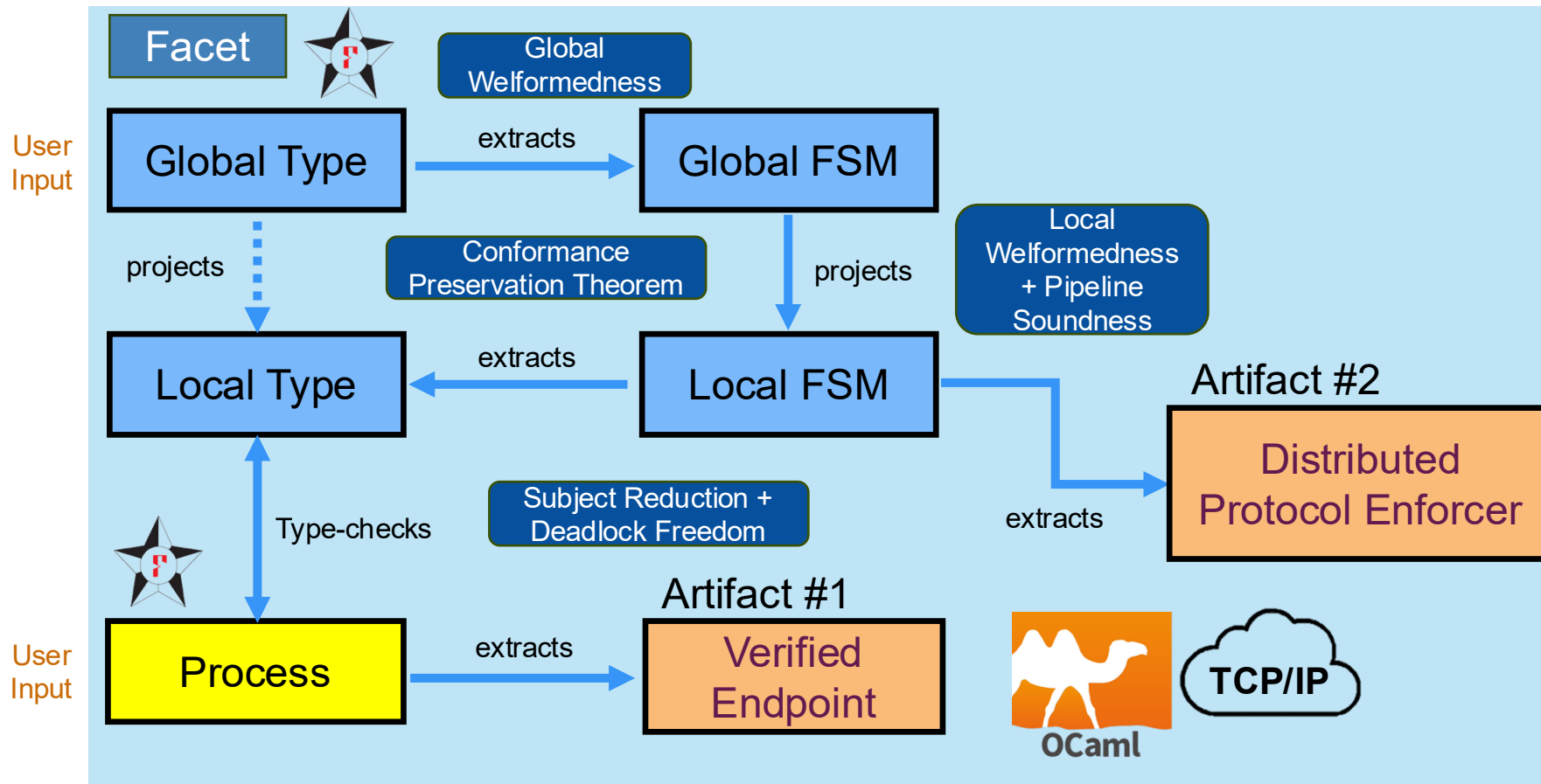


First mechanized RMPST metatheory

Proofs (e.g. absence of deadlocks) just by using our DSL

Facet: Mechanized RMPST metatheory in F*

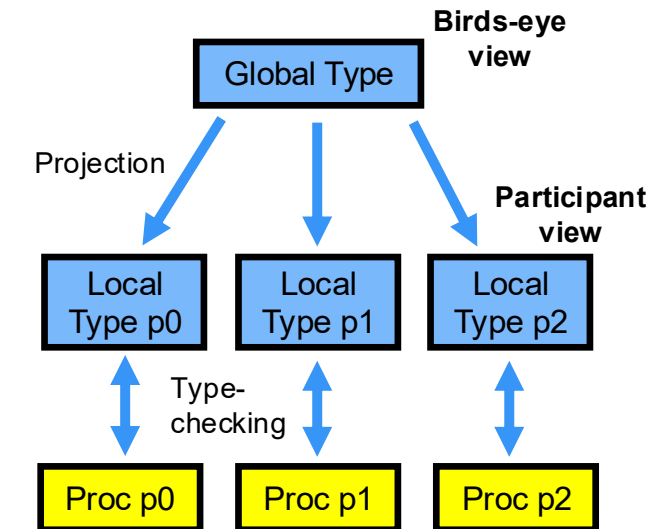
1- Semantic Gap



Facet

(RMPSTs)

Refined Multiparty Session Types



First mechanized RMPST metatheory

Proofs (e.g. absence of deadlocks)
just by using our DSL

Facet Closes the Semantic Gap With Mechanized Metatheory

Artifact #1

Verified Endpoint

Projection



```

Server → Auth : PIN (expected_code :  $\mathbb{Z}$  {expected_code ≥ 0 ∧ expected_code ≤ 999999})
μ.T(count :  $\mathbb{Z}$ {0 < count ∧ count ≤ 5}) 1

Auth → User : RequestAuth ( _ : unit)
User → Auth : SubmitCode (submitted :  $\mathbb{Z}$  {submitted ≥ 0 ∧ submitted ≤ 999999})

Auth → User : {
  Success ( _ : unit {submitted = expected_code}).End
  Failed ( _ : unit {submitted ≠ expected_code ∧ count < 5}).T(count + 1)
  Locked ( _ : unit {submitted ≠ expected_code ∧ count = 5}).End
}
    
```

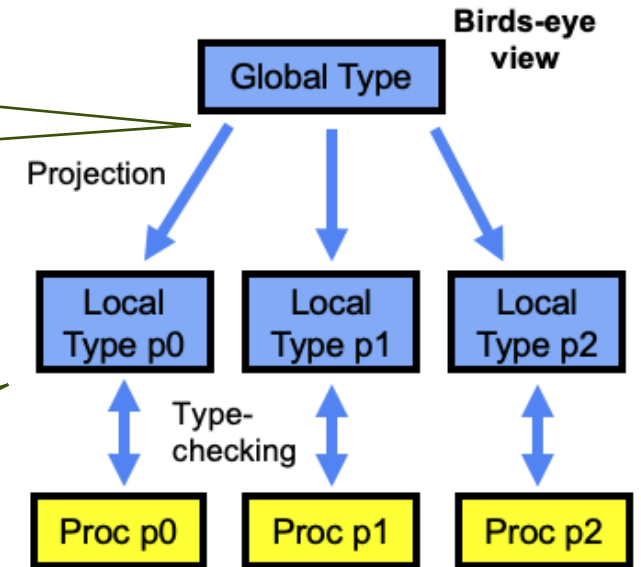
```

μ. L(count :  $\mathbb{Z}$ {0 < count ≤ 5}) :
? Auth : RequestAuth ( _ : unit);
! Auth : SubmitCode (submitted :  $\mathbb{Z}$  {submitted ≥ 0 ∧ submitted ≤ 999999});
& Auth : { Success ( _ : unit).End | Failed ( _ : unit).L(count + 1) | Locked ( _ : unit).End}
    
```

Messages are **statically** verified against refinements

```

let authenticator_p1 : process =
  Recv 0 [
    ("PIN" ==> fun (expected:int{expected > 0 && expected <= 999999}) ->
      Loop 1 (fun (count:int{count > 0 && count <= 5}) ->
        Send 2 [
          always_send "RequestAuth" () (
            Recv 2 [
              ("SubmitCode" ==> fun (code:int{code >= 0 && code <= 999999}) ->
                Send 2 [
                  send "Success"
                    (fun () -> code = expected)
                  ()
                ]
              Done;
            )
          ]
        )
      )
  ]
    
```



Built-in Proofs

- 1- Absence of Deadlocks
- 2- Guarded Recursion
- 3- Session Fidelity
- 4- Label Uniqueness

Facet Closes the Semantic Gap With Mechanized Metatheory

Artifact #2

Distributed Protocol Enforcer

Projection



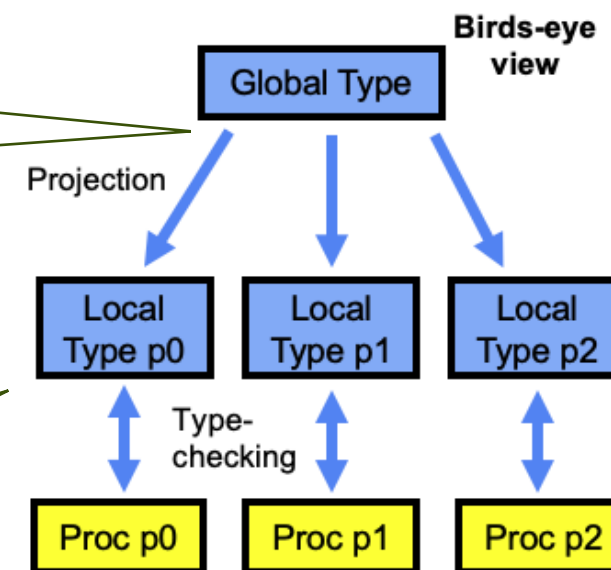
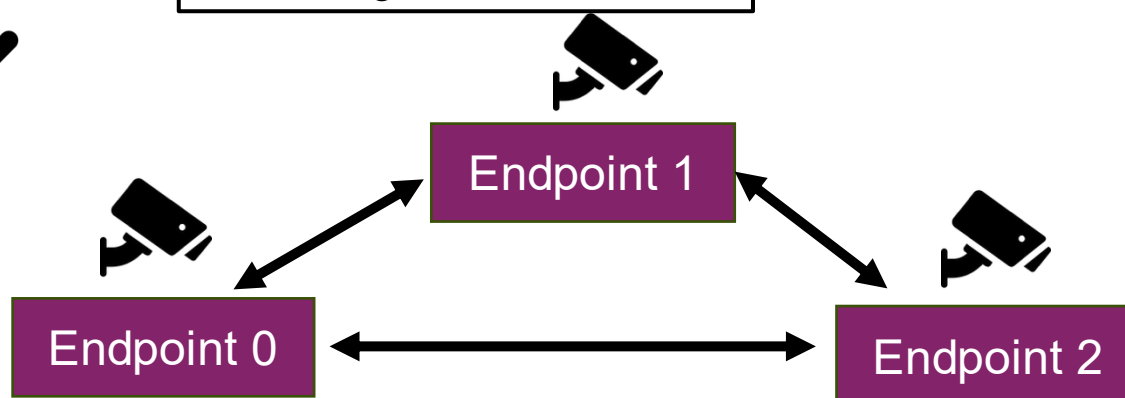
```

Server → Auth : PIN (expected_code :  $\mathbb{Z}$  {expected_code  $\geq$  0  $\wedge$  expected_code  $\leq$  999999})
 $\mu.T(count : \mathbb{Z}\{0 < count \wedge count \leq 5\})$  1
Auth → User : RequestAuth (_ : unit)
User → Auth : SubmitCode (submitted :  $\mathbb{Z}$  {submitted  $\geq$  0  $\wedge$  submitted  $\leq$  999999})
Auth → User : {
  Success (_ : unit {submitted = expected_code}).End
  Failed (_ : unit {submitted  $\neq$  expected_code  $\wedge$  count < 5}).T(count + 1)
  Locked (_ : unit {submitted  $\neq$  expected_code  $\wedge$  count = 5}).End
}
    
```

```

 $\mu.L(count : \mathbb{Z}\{0 < count \leq 5\})$  :
? Auth : RequestAuth (_ : unit);
! Auth : SubmitCode (submitted :  $\mathbb{Z}$  {submitted  $\geq$  0  $\wedge$  submitted  $\leq$  999999});
& Auth : { Success (_ : unit).End | Failed (_ : unit).L(count + 1) | Locked (_ : unit).End}
    
```

Messages are **dynamically** verified against refinements



Built-in Proofs

- 1- Absence of Deadlocks
- 2- Guarded Recursion
- 3- Session Fidelity
- 4- Label Uniqueness

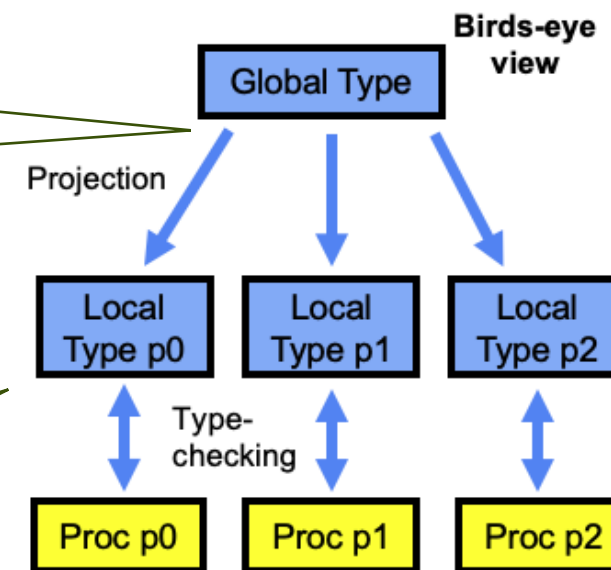
Facet Closes the Semantic Gap With Mechanized Metatheory

```

Server → Auth : PIN (expected_code :  $\mathbb{Z} \{ \text{expected\_code} \geq 0 \wedge \text{expected\_code} \leq 999999 \}$ )
 $\mu.T(\text{count} : \mathbb{Z} \{ 0 < \text{count} \wedge \text{count} \leq 5 \}) 1$ 
Auth → User : RequestAuth ( _ : unit)
User → Auth : SubmitCode (submitted :  $\mathbb{Z} \{ \text{submitted} \geq 0 \wedge \text{submitted} \leq 999999 \}$ )
Auth → User : {
  Success ( _ : unit {submitted = expected_code}).End
  Failed ( _ : unit {submitted  $\neq$  expected_code  $\wedge$  count < 5}).T(count + 1)
  Locked ( _ : unit {submitted  $\neq$  expected_code  $\wedge$  count = 5}).End
}
    
```

```

 $\mu. L(\text{count} : \mathbb{Z} \{ 0 < \text{count} \leq 5 \}) :$ 
? Auth : RequestAuth ( _ : unit);
! Auth : SubmitCode (submitted :  $\mathbb{Z} \{ \text{submitted} \geq 0 \wedge \text{submitted} \leq 999999 \}$ );
& Auth : { Success ( _ : unit).End | Failed ( _ : unit).L(count + 1) | Locked ( _ : unit).End}
    
```



Artifact #1

Verified Endpoint

Messages are **statically** verified against refinements

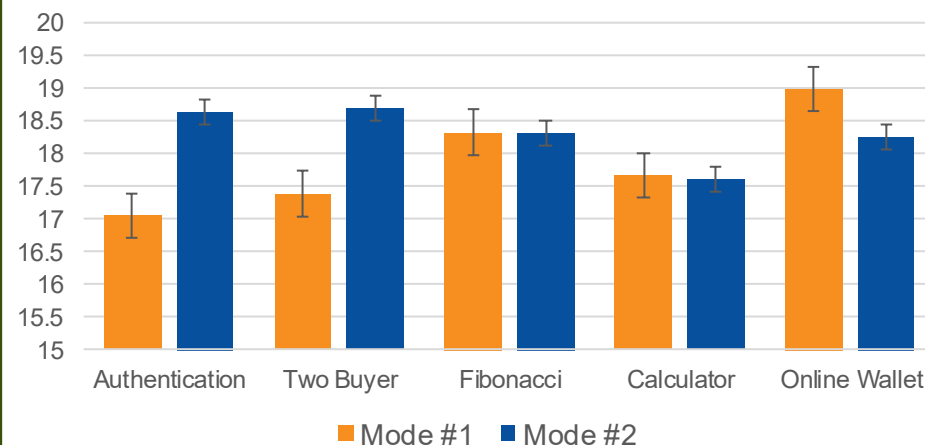
Artifact #2

Distributed Protocol Enforcer

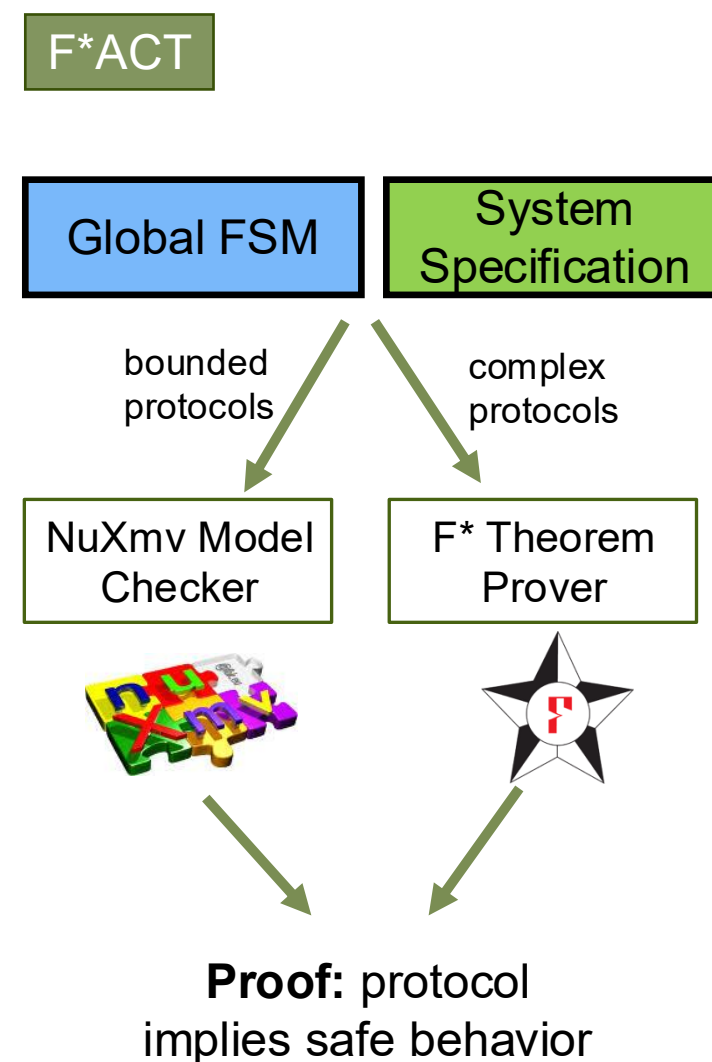
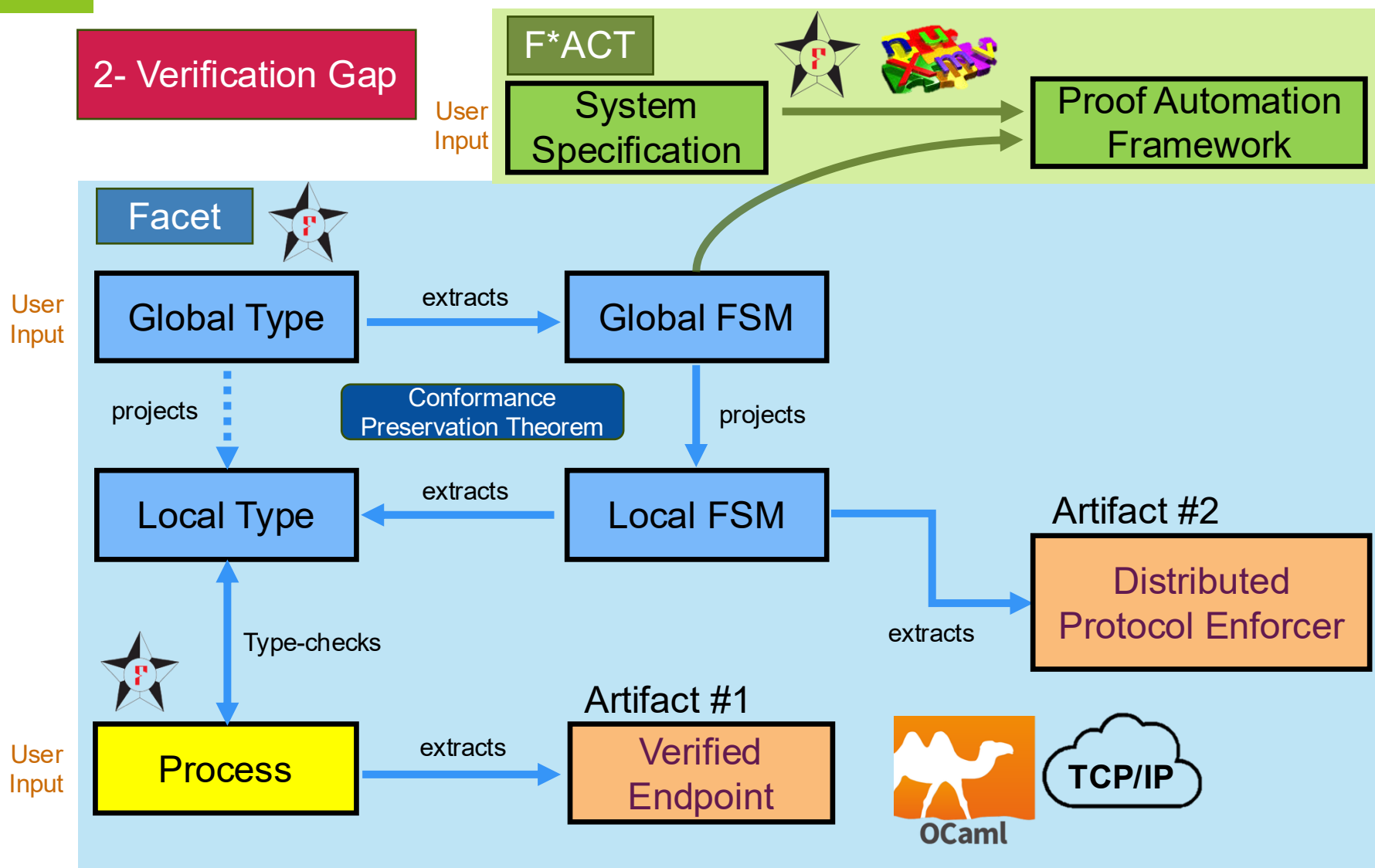


Messages are **dynamically** verified against refinements

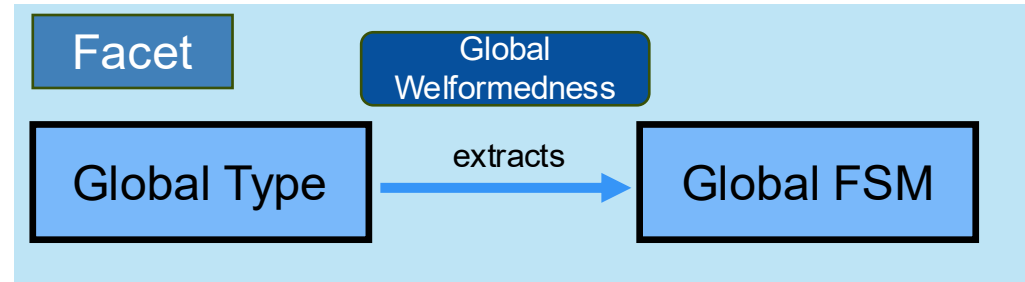
Runtime Overhead of Artifacts(ms)



F*ACT: Automated and Scalable Proof Methods.



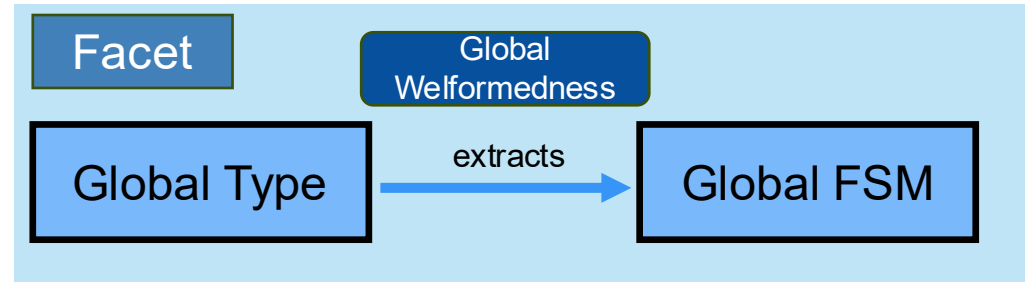
The Engine That Makes This Tractable: Shallow-to-Deep Embedding Extraction



RMPST

```
GCS → UAV: MISSION COUNT( $n\{1 \leq n < \text{LIMIT}\}$ )  
 $\mu.T(\text{curr}\{0 \leq \text{curr} < n\})(\text{curr} = 0)$   
UAV → GCS:  
  MISSION REQUEST INT( $\text{req}\{\text{req} = \text{curr} < n\}$ )  
  MISSION ITEM INT( $\text{item}\{\text{item} = \text{curr} < n\}$ )  
   $T(\text{curr} + 1)$   
 $\oplus$  MISSION ACK( $\text{ack}\{\text{type} = \text{ERROR} \vee \text{curr} = n\}$ ).End
```

The Engine That Makes This Tractable: Shallow-to-Deep Embedding Extraction

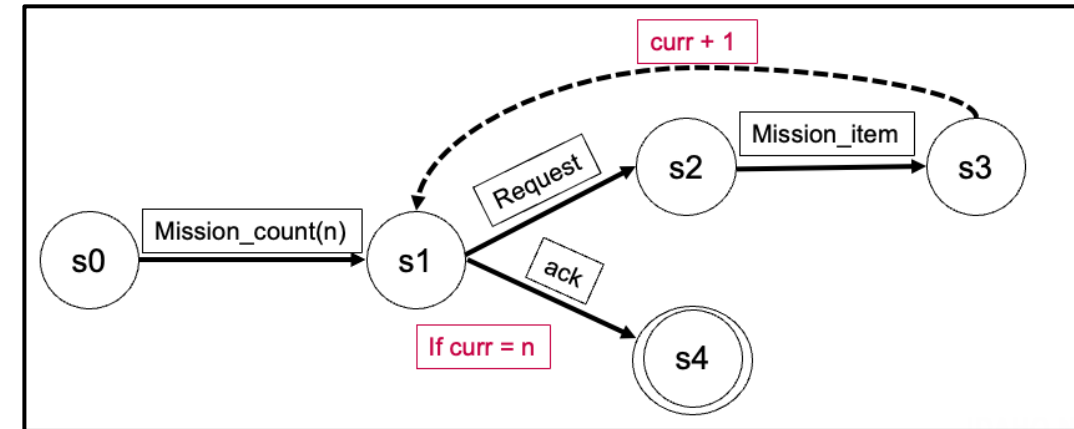


RMPST

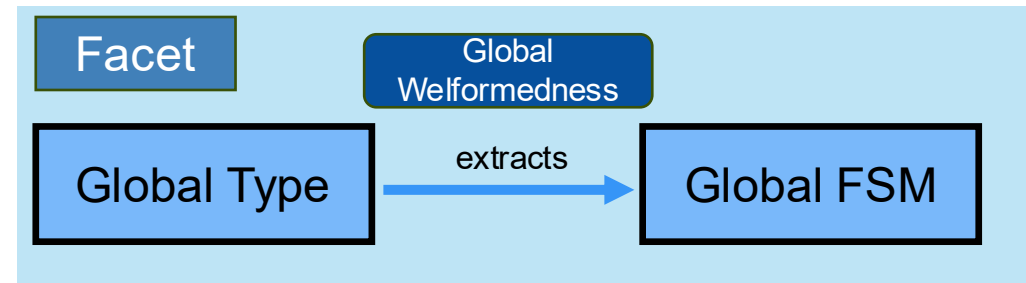
```

GCS → UAV: MISSION COUNT( $n\{1 \leq n < \text{LIMIT}\}$ )
 $\mu.T(\text{curr}\{0 \leq \text{curr} < n\})(\text{curr} = 0)$ 
UAV → GCS:
  MISSION REQUEST INT( $\text{req}\{\text{req} = \text{curr} < n\}$ )
  MISSION ITEM INT( $\text{item}\{\text{item} = \text{curr} < n\}$ )
   $T(\text{curr} + 1)$ 
 $\oplus$  MISSION ACK( $\text{ack}\{\text{type} = \text{ERROR} \vee \text{curr} = n\}$ ).End
  
```

Proof Internal



The Engine That Makes This Tractable: Shallow-to-Deep Embedding Extraction

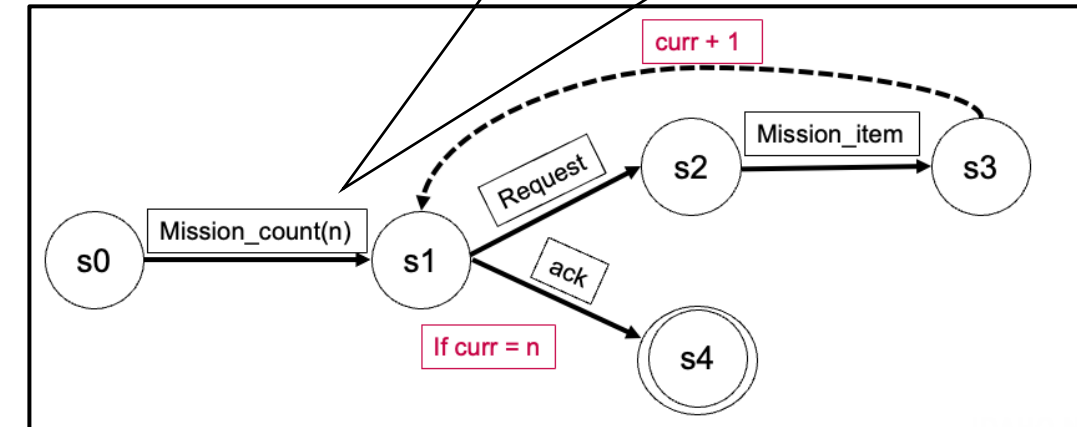


```
Mkprotocol_transition "MISSION_COUNT" 0 1
[
  Mkvar "mc_target_system" KindInt;
  Mkvar "mc_target_component" KindInt;
  Mkvar "mc_count" KindInt;
  Mkvar "mc_mission_type" KindInt;
  Mkvar "mc_opaque_id" KindInt
]
(GAnd (GGe (TVar "mc_count") (TIntLit
1))) (GLt (TVar "mc_count") (TIntLit 65535)))
```

RMPST

```
GCS → UAV: MISSION COUNT( $n\{1 \leq n < \text{LIMIT}\}$ )
 $\mu.T(\text{curr}\{0 \leq \text{curr} < n\})(\text{curr} = 0)$ 
UAV → GCS:
  MISSION REQUEST INT( $\text{req}\{\text{req} = \text{curr} < n\}$ )
  MISSION ITEM INT( $\text{item}\{\text{item} = \text{curr} < n\}$ )
   $T(\text{curr} + 1)$ 
 $\oplus$  MISSION ACK( $\text{ack}\{\text{type} = \text{ERROR} \vee \text{curr} = n\}$ ).End
```

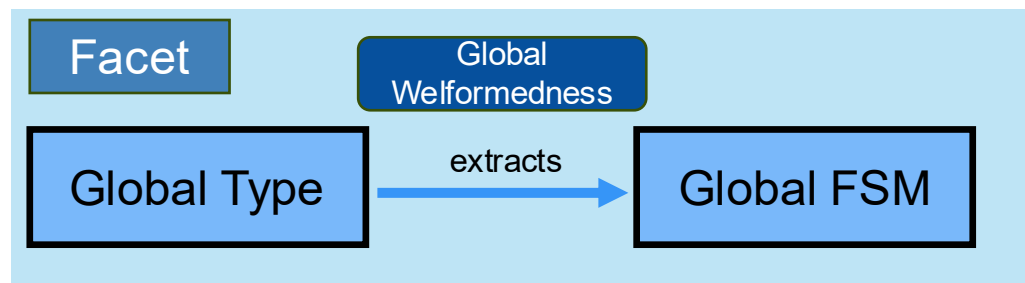
Proof Internal



Our DSL:

```
(0 --> 1) [Option "MISSION_COUNT" (λ (cnt : mission_count { cnt >= 1 && cnt < mission_limit})
```

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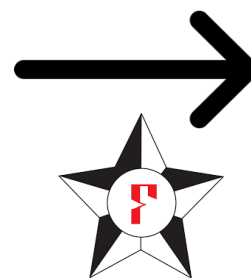
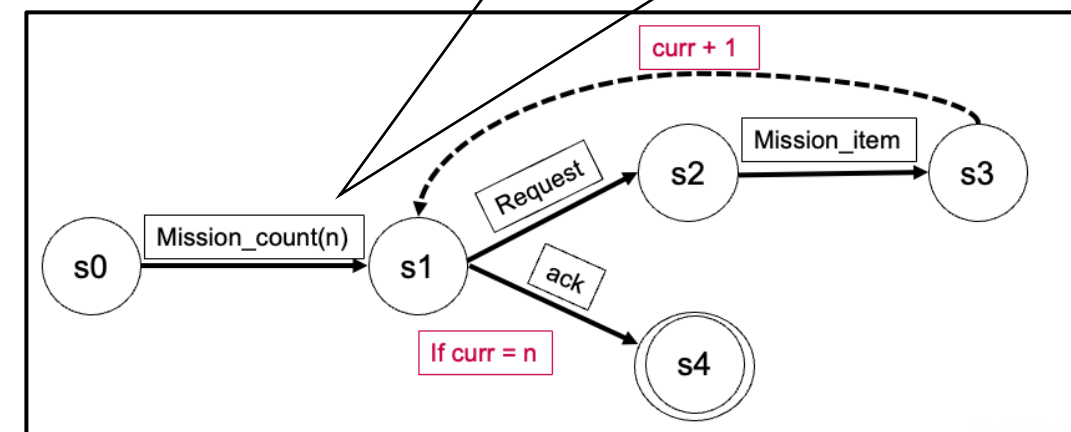


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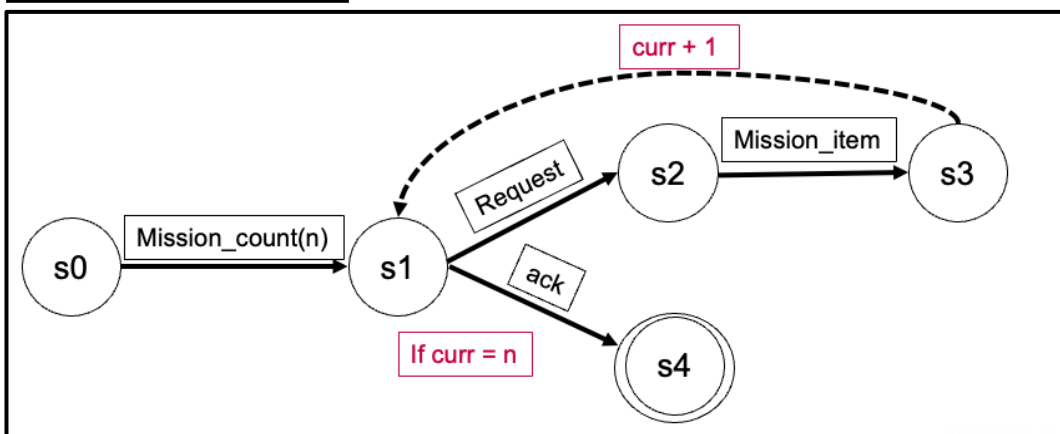
Meta-F*

Our DSL:

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F*ACT Proves Application-Specific Safety Without State Explosion

Global FSM



System Specification

Safety Properties + System Semantics

- "The GCS must send all missions in order without skips"
- "An ack(success) message can only be sent when $curr = n$ "

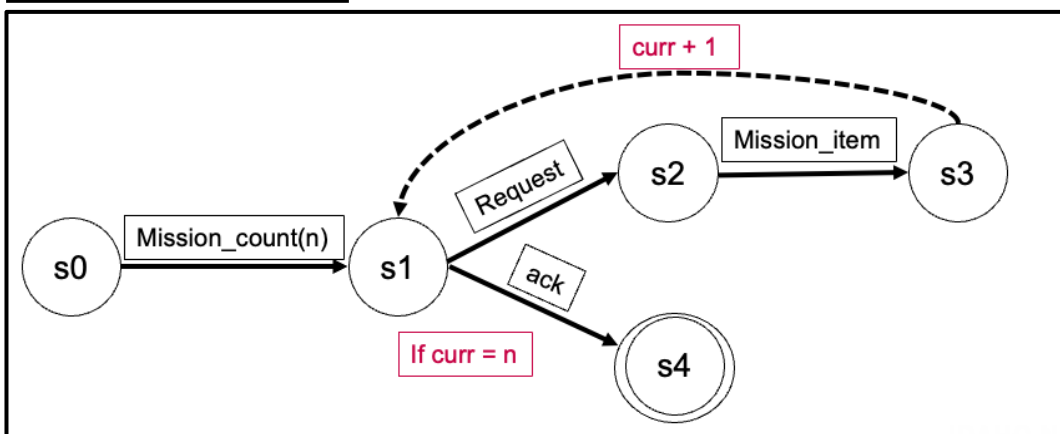
Operational Semantics

State + Command $\rightarrow$ *State*

Valid State | **WRONG**

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Global FSM



System Specification

- "The GCS must send all missions in order without skips"
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Operational Semantics

$(n = 10; m = 13) + \text{Succeed} \rightarrow \text{WRONG}$

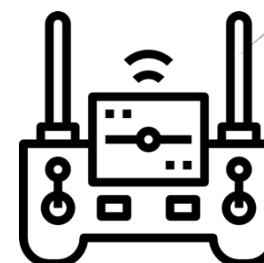
Safety Condition: following a protocol must never lead the system to a WRONG state

Mission 1:
Count = 10

Buffer
6 7 8 9



UAV



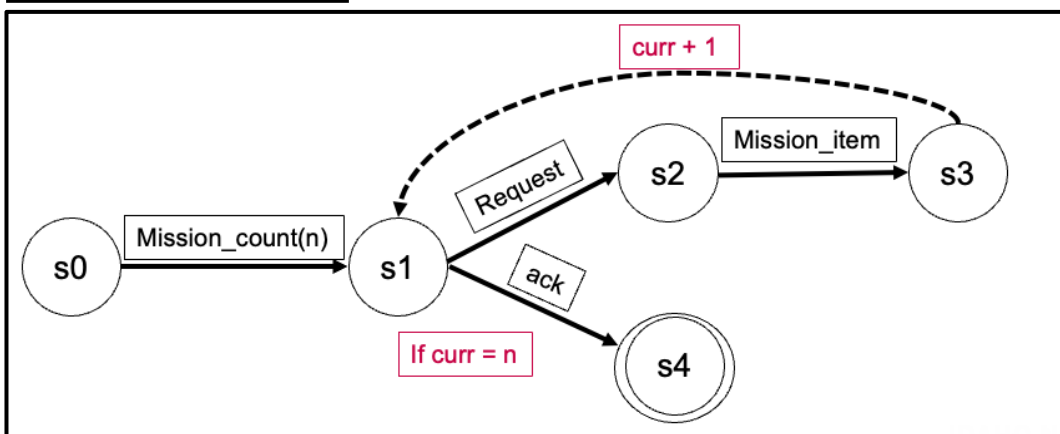
GCS



F*ACT Proves Application-Specific Safety Without State Explosion

Model Checking

Global FSM



- 1- Variables
- 2- Initial values
- 3- States (variable updates)
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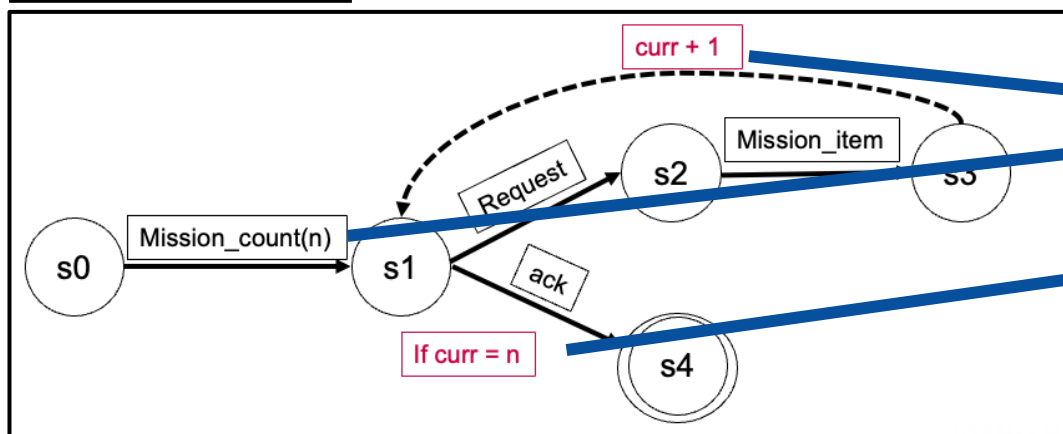
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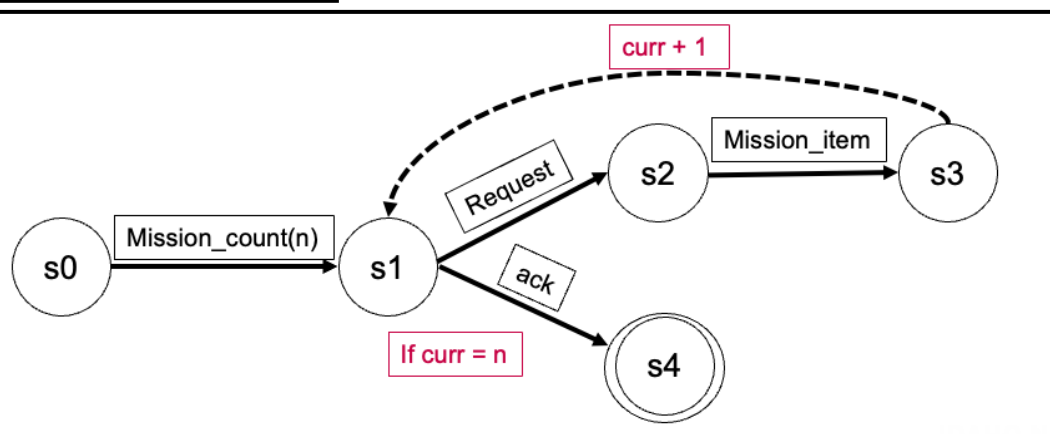
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Meta-F*

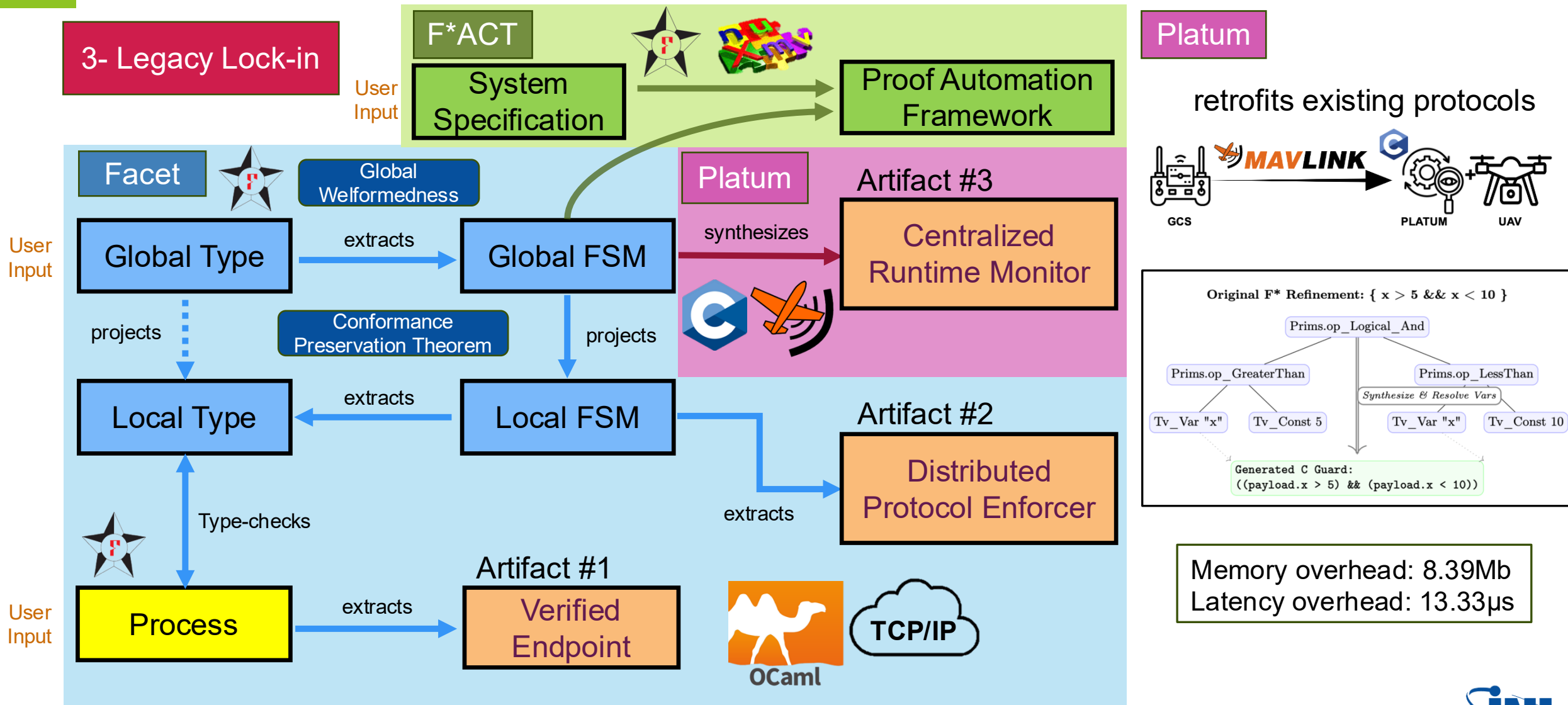


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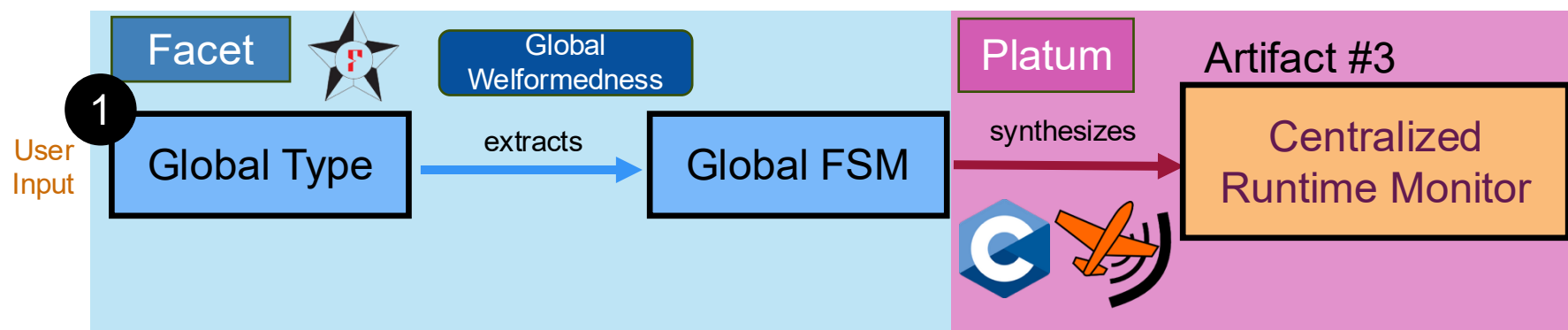
Theorem proving

Safety Condition: following a protocol must never lead the system to a WRONG state

Platum: Verified Runtime Monitors for Legacy Protocols.



Platum Retrofits Legacy Protocols Without Replacing Them

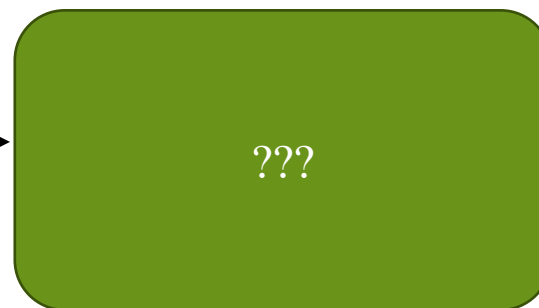


MAVLink spec

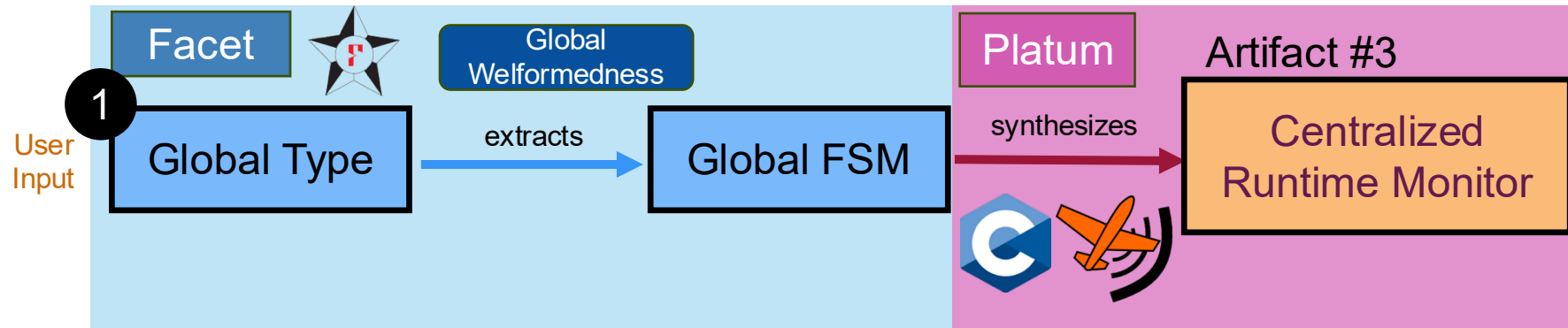


Common.xml

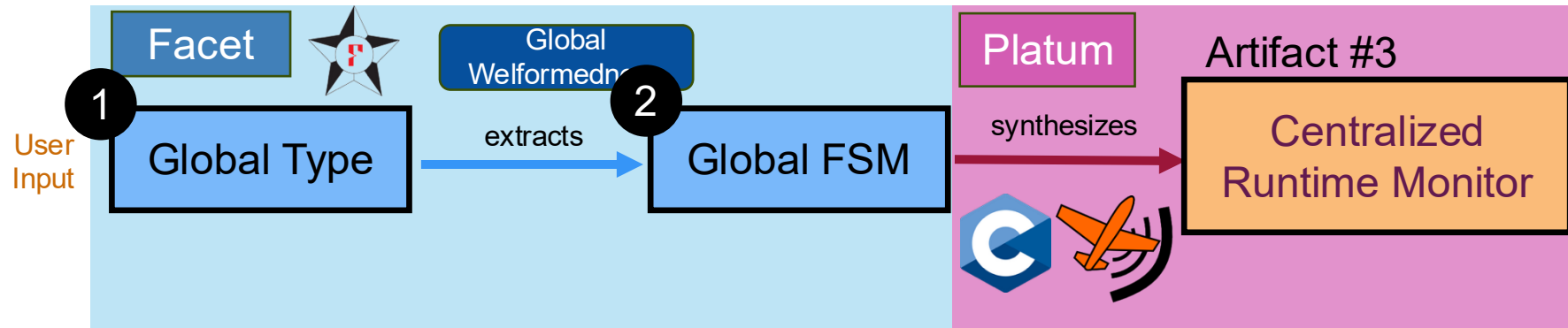
```
<message
name="MISSION_COUNT">
<field type="uint16_t"
name="count">
</field>
</message>
```



Platum Retrofits Legacy Protocols Without Replacing Them



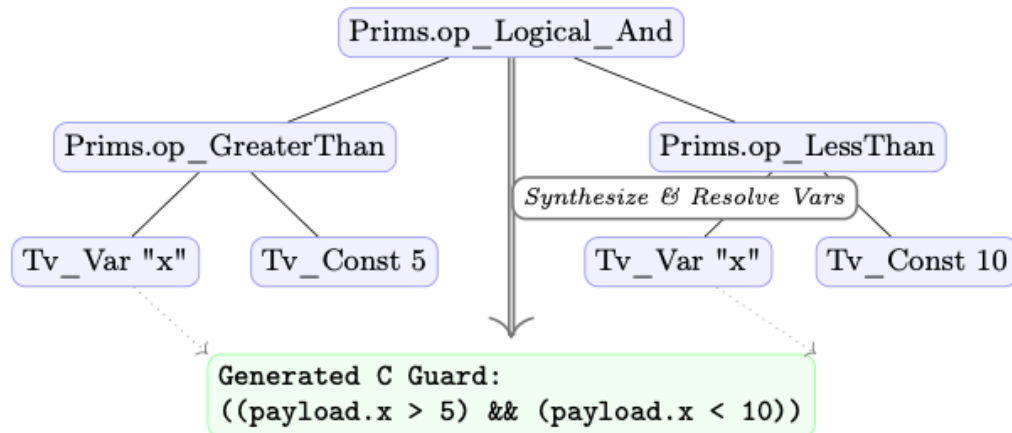
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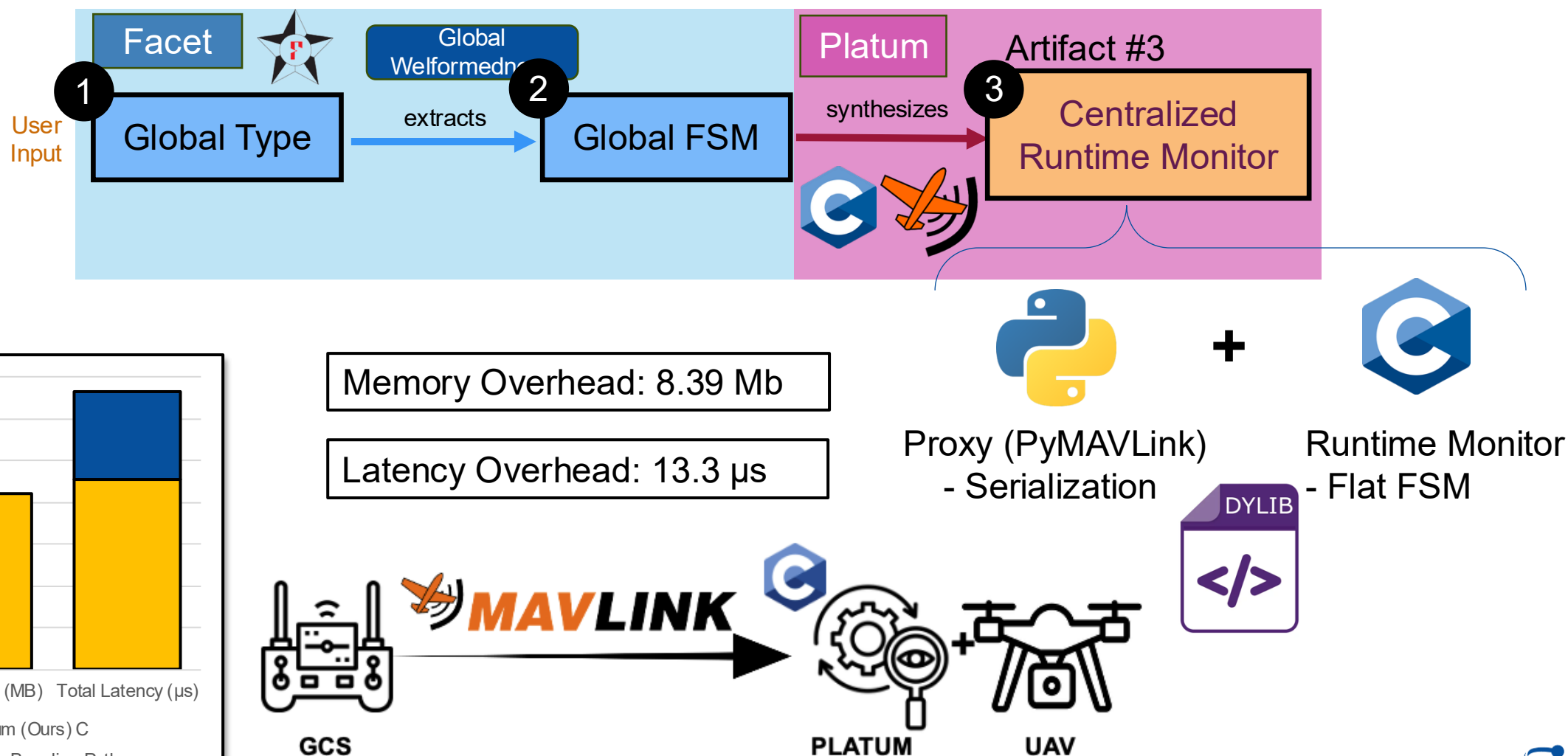
$(cnt : mission_count \{ cnt \geq 1 \ \&\& \ cnt < mission_limit \})$

Type Erasure

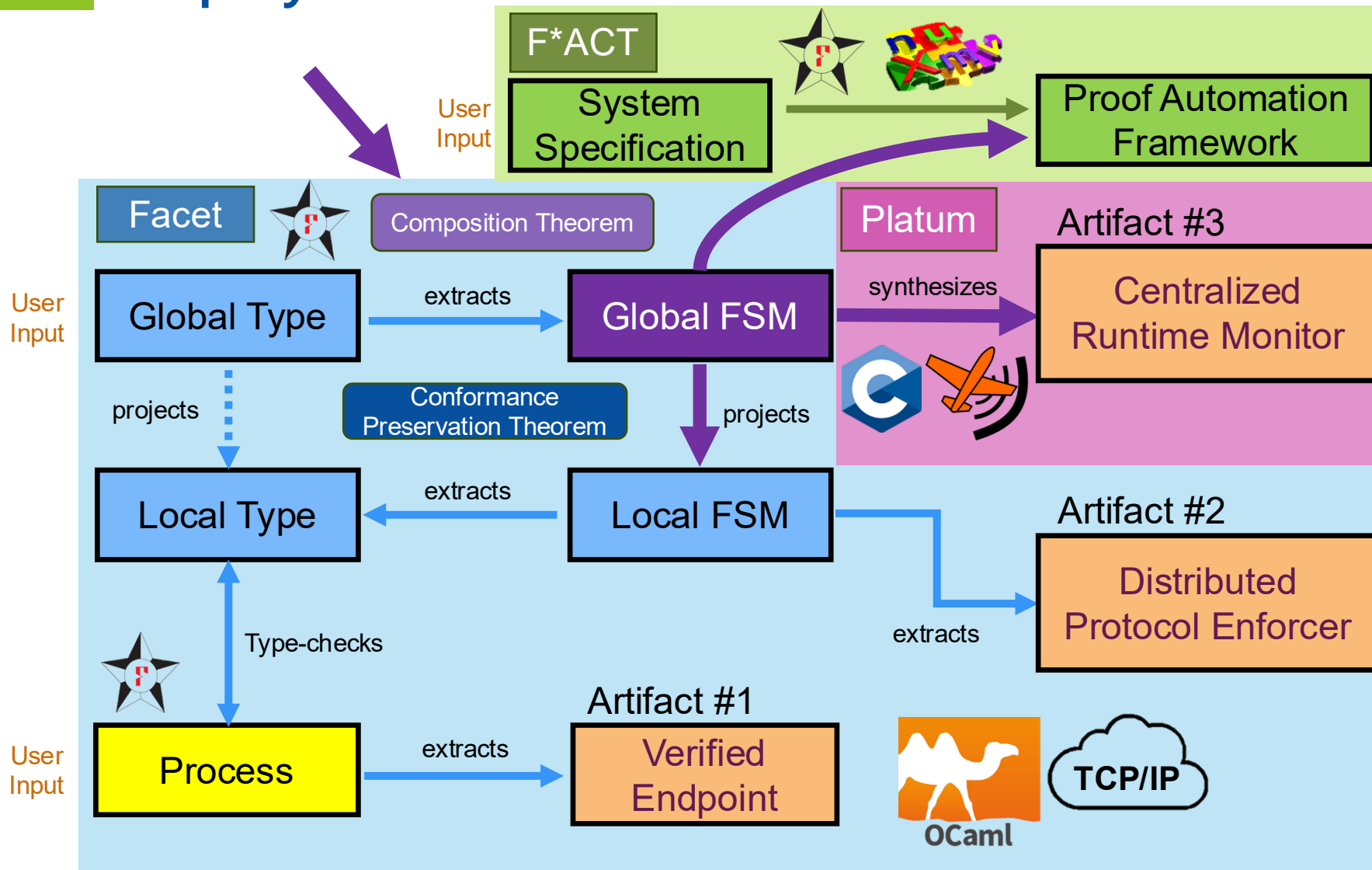
Original F* Refinement: $\{ x > 5 \ \&\& \ x < 10 \}$



Platum Retrofits Legacy Protocols Without Replacing Them

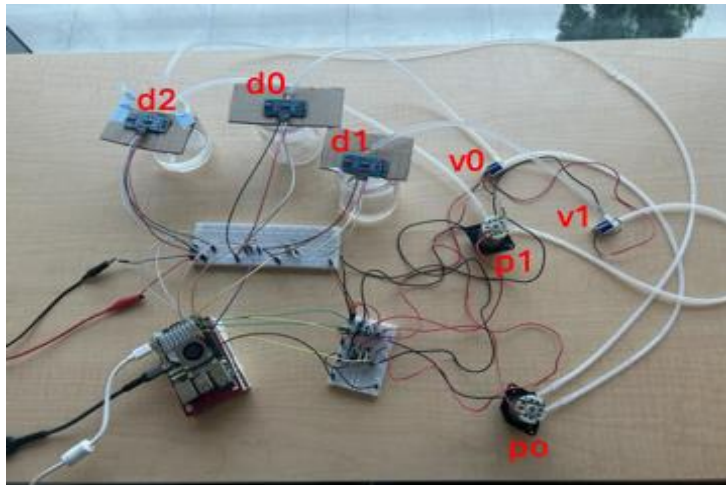
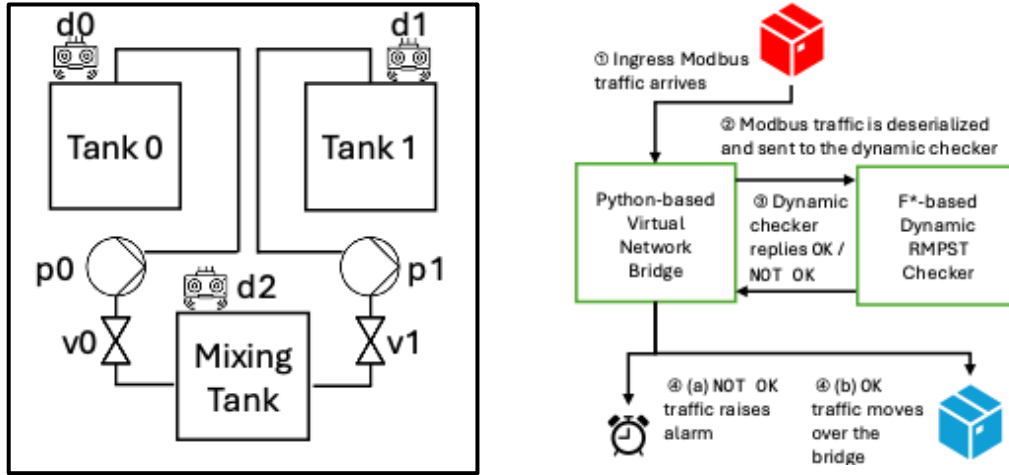


A Single Certified Semantic Model Shared Across All Generated Deployment Artifacts



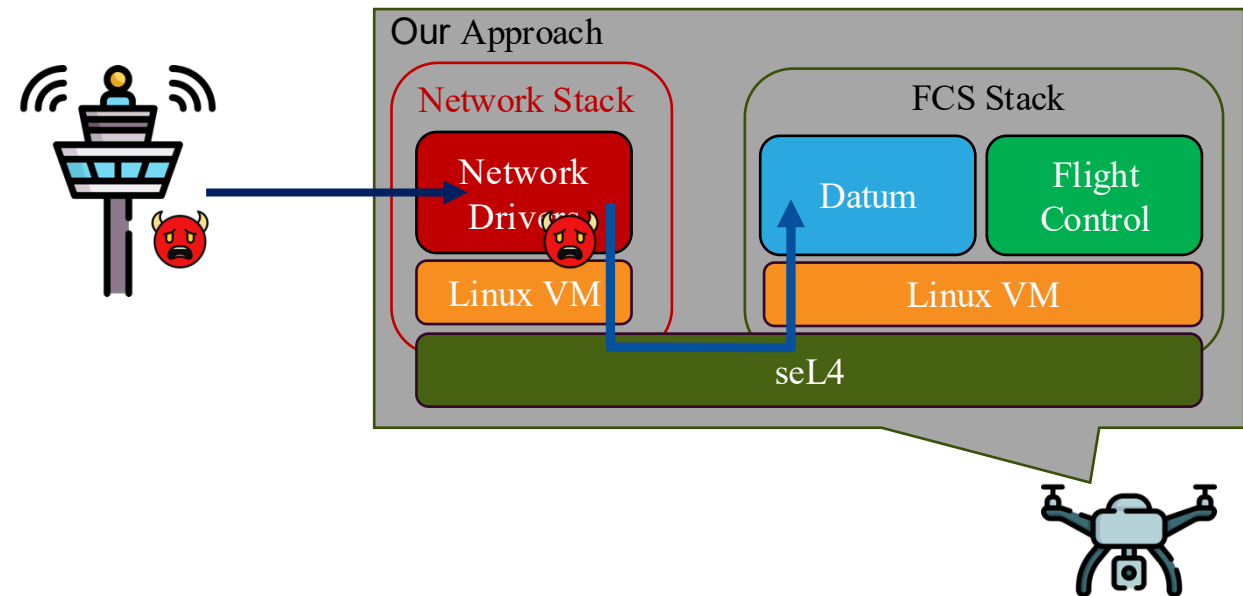
Previous Deployments

Modbus-based industrial control system ⁴



4- Max Taylor and Arthur Amorim. Securing Modbus-Based Industrial Control Systems with Refined Multiparty Session Types. VERDI'25

Integrated Datum(predecessor) with Sel4 to protect against stronger threat model.⁵



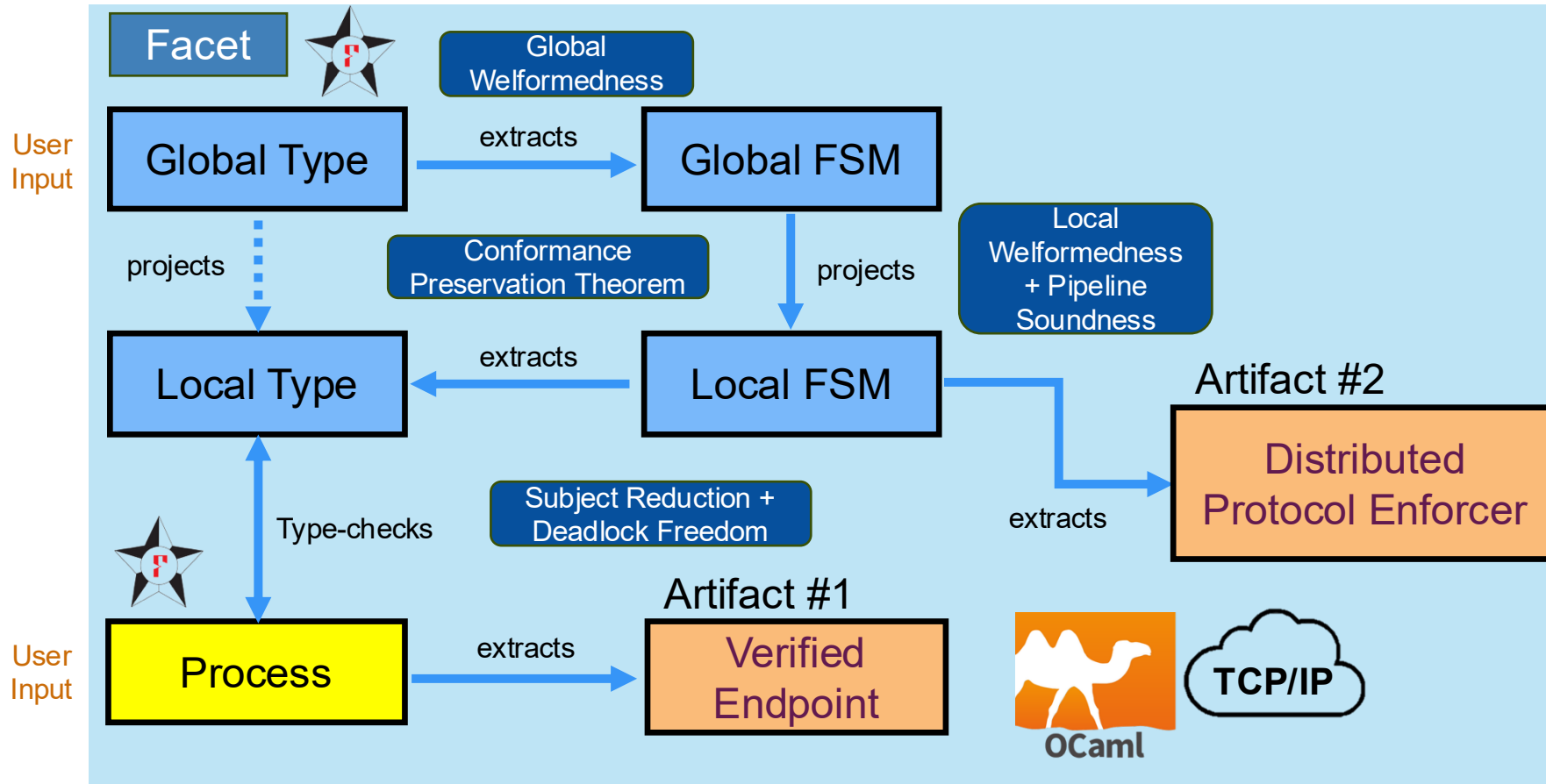
5- Arthur Amorim et al. UAV Resilience Against Stealthy Attacks. ICUAS'25

One Verified Model, Three Certified Artifacts

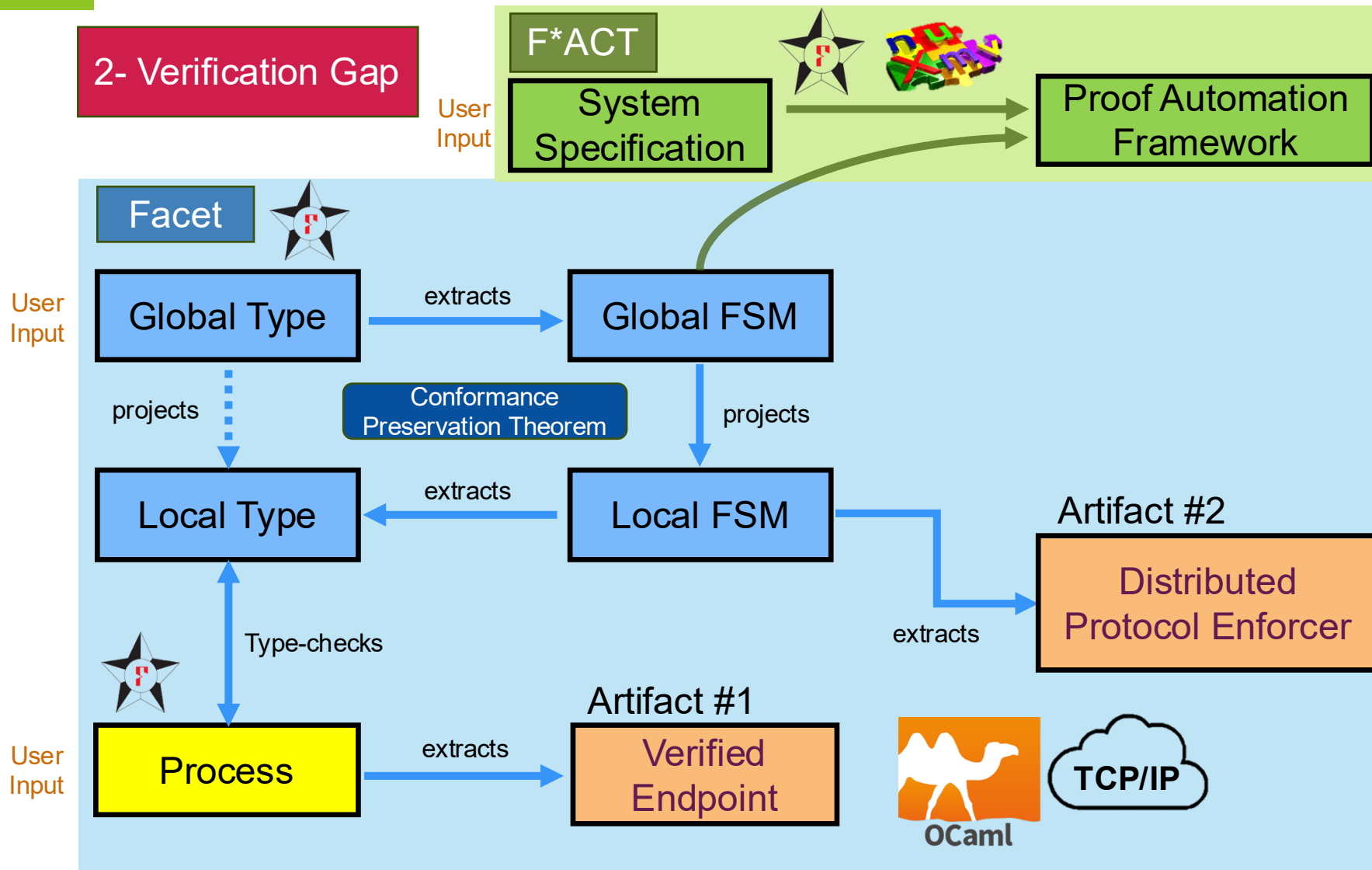
1- Semantic Gap

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Facet: first mechanized RMPST metatheory; the proof and the runtime enforcer are the same object



One Verified Model, Three Certified Artifacts



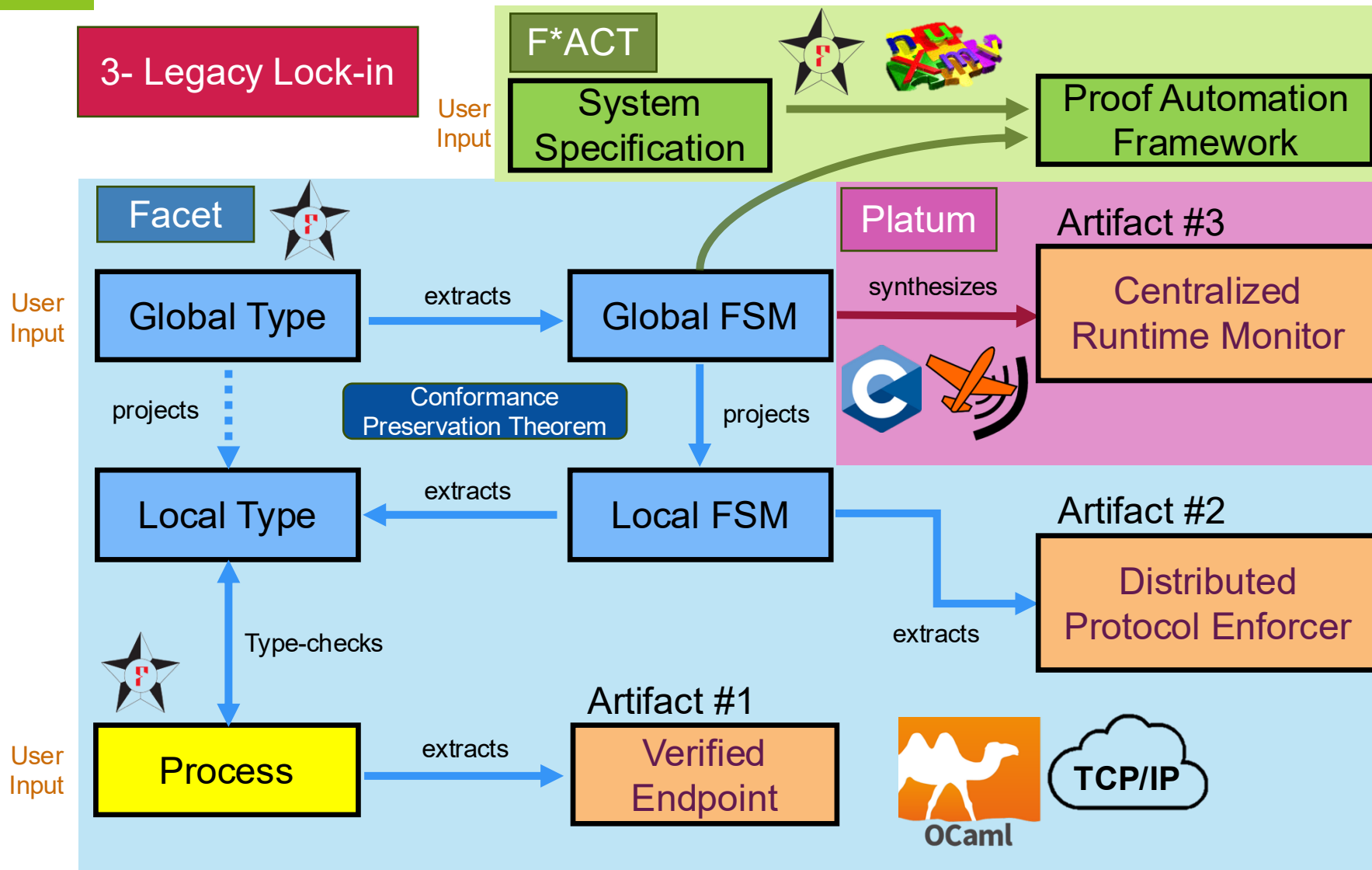
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2- Proof Celling

F*ACT: combines automated model checking with tactic-based certificate generation for complex protocols

One Verified Model, Three Certified Artifacts



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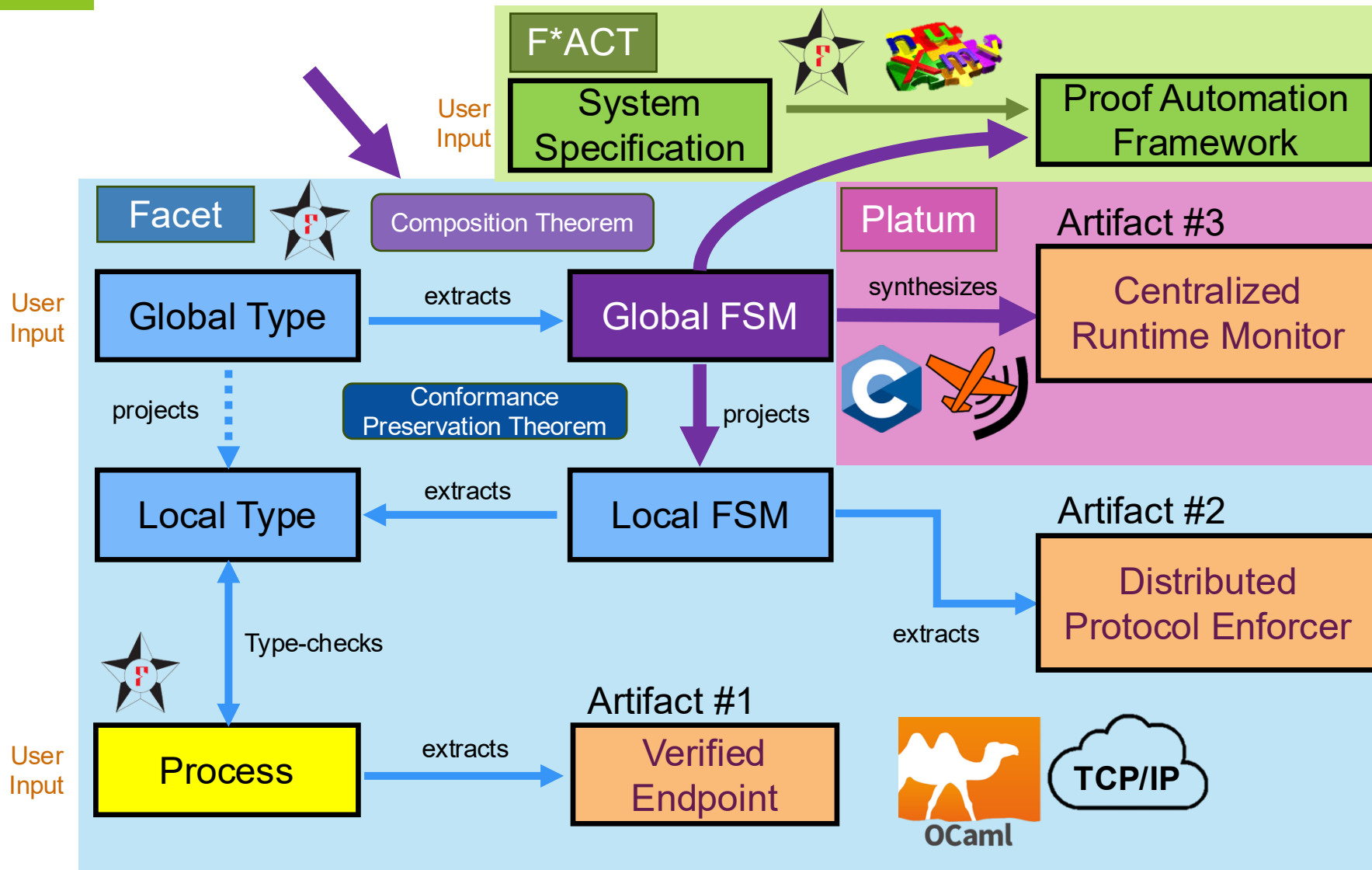
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Platum: synthesizes verified C monitors that retrofit any existing protocol without touching the endpoints

One Verified Model, Three Certified Artifacts



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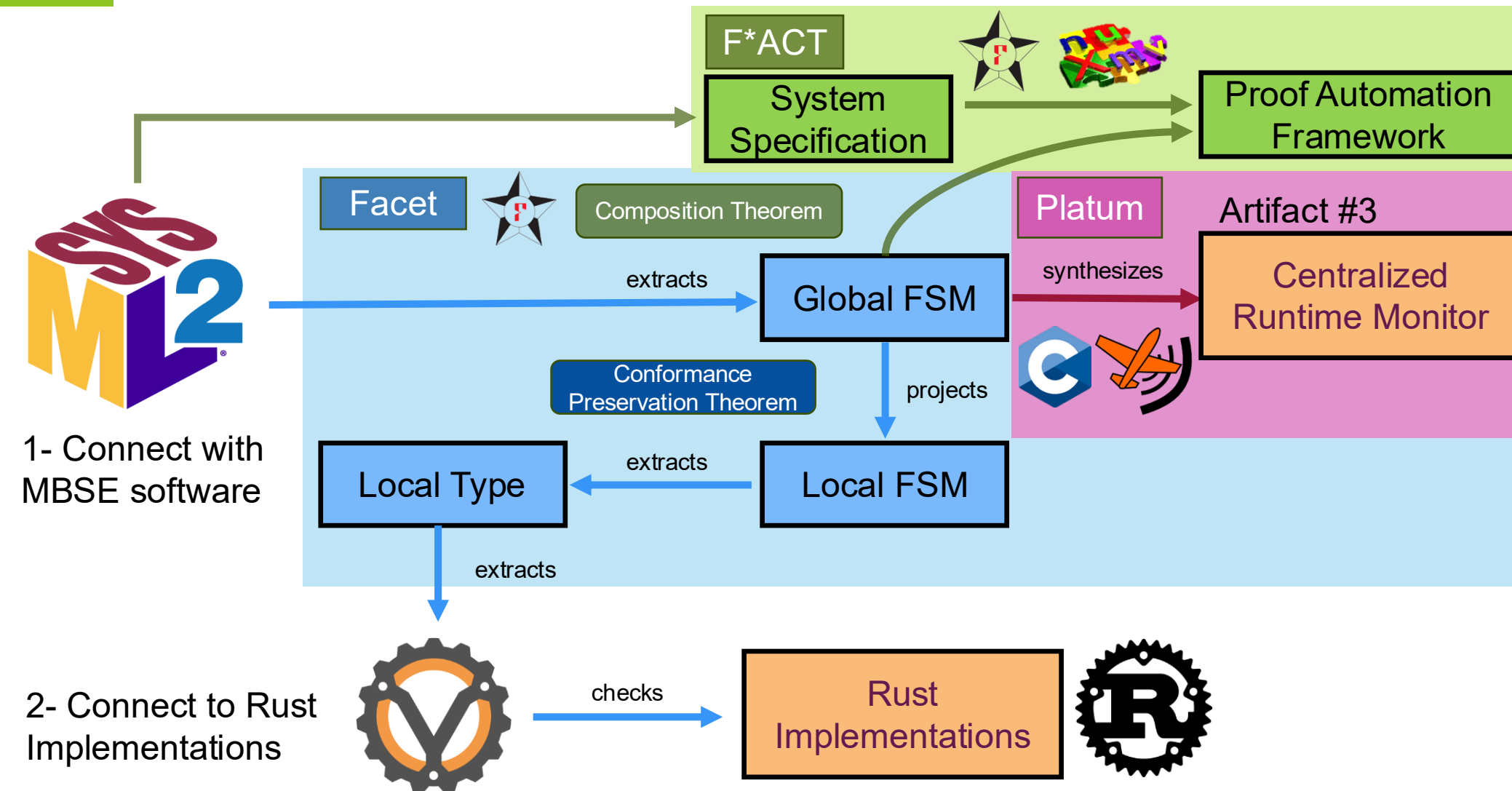
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Future Directions

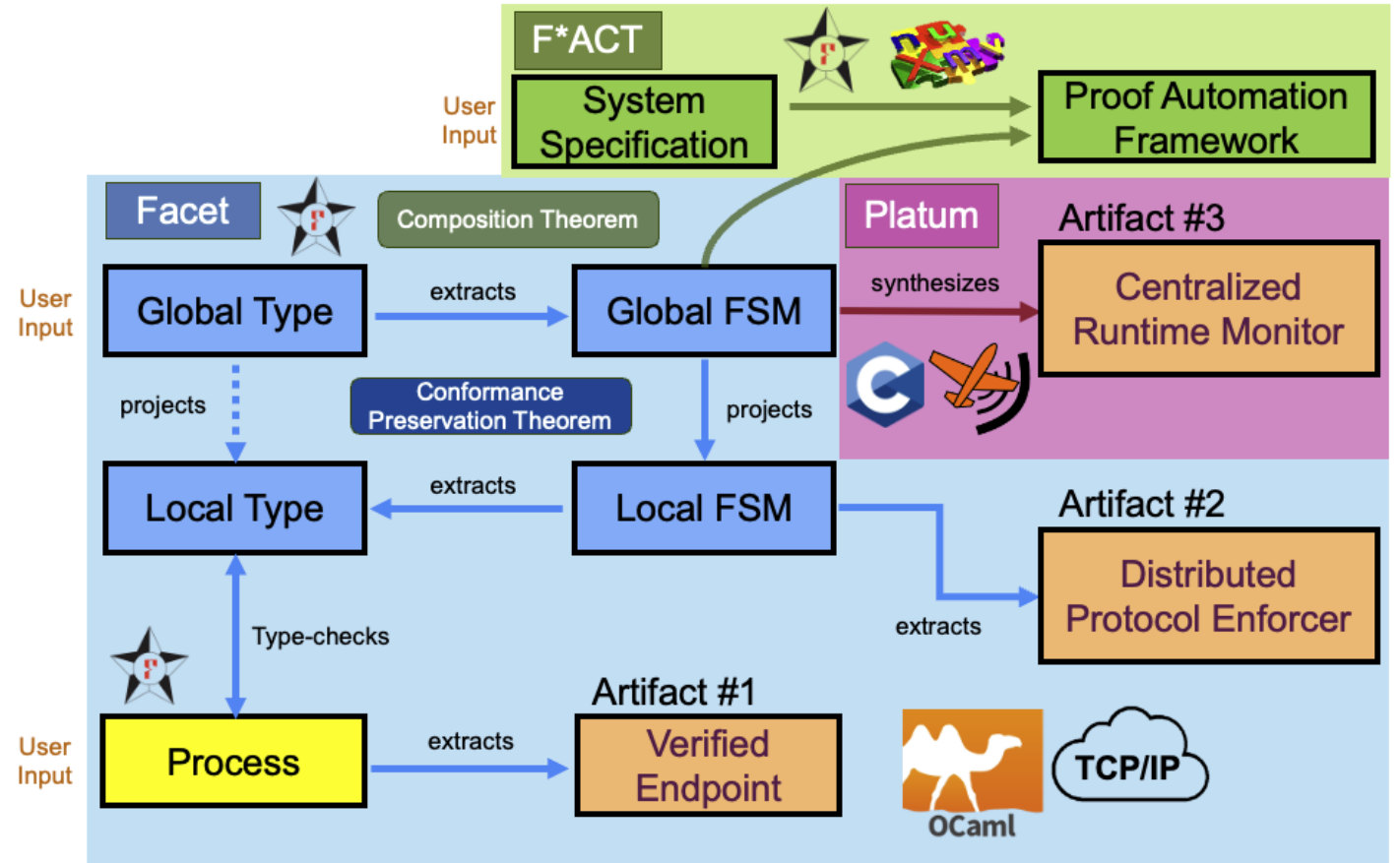


One Verified Model, Three Certified Artifacts

OPEN TO WORK



Arthur Amorim
arthur.amorim@ucf.edu
arthur.amorim@inl.gov
Website



1- Semantic Gap

Facet: first mechanized RMPST metatheory; the proof and the runtime enforcer are the same object

2- Verification gap

F*ACT: combines automated model checking with tactic-based certificate generation for complex protocols

3- Legacy Lock-in

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Why F*?

Z3

- Z3 automatically discharges proof obligations in its decision procedures
- Makes it practical to use operational semantics

- Native, first-class refinements $\{x : T \mid \varphi(x)\}$
- RMPSTs map directly to F* refinement types

Server $\rightarrow$ **Auth** : **PIN** ($expected_code : \mathbb{Z} \{expected_code \geq 0 \wedge expected_code \leq 999999\}$)

$\mu.T(count : \mathbb{Z}\{0 < count \wedge count \leq 5\})$ 1

Auth $\rightarrow$ **User** : **RequestAuth** ($_ : unit$)

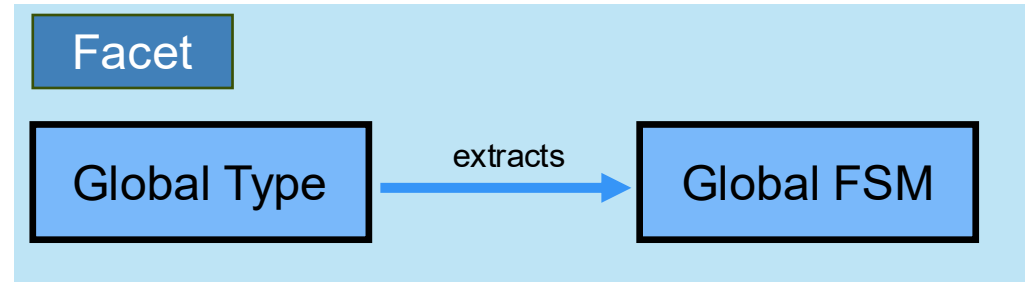
User $\rightarrow$ **Auth** : **SubmitCode** ($submitted : \mathbb{Z} \{submitted \geq 0 \wedge submitted \leq 999999\}$)

Auth $\rightarrow$ **User** : $\begin{cases} \text{Success } (_ : unit \{submitted = expected_code\}).\text{End} \\ \text{Failed } (_ : unit \{submitted \neq expected_code \wedge count < 5\}).T(count + 1) \\ \text{Locked } (_ : unit \{submitted \neq expected_code \wedge count = 5\}).\text{End} \end{cases}$



- Principled extraction pipeline to high-performance languages
- Project Everest: Verified TLS 1.3 in production

The Engine That Makes This Tractable: Shallow-to-Deep Embedding Extraction



Shallow embedding:

- Easy to write (uses host language)
- hard to prove (must reason about all of F^*)

```
(0 --> 1) [ Option "Counter" (fun (count : int  
{count > 0 && count <= 5})
```

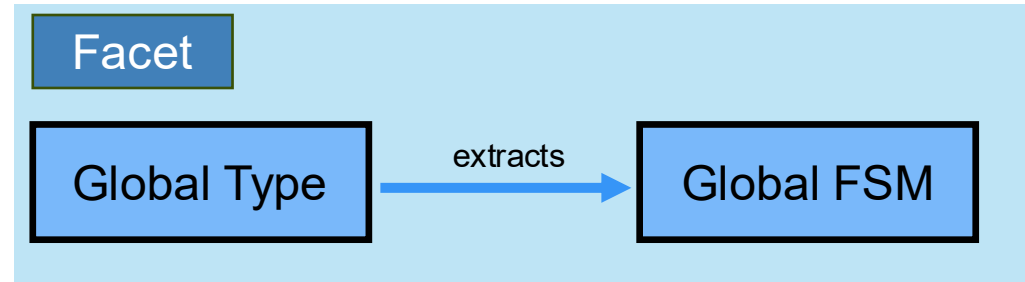
VS

Deep embedding:

- Hard to write (explicit syntax trees),
- Easy to prove (reason only about DSL)

```
Mkmu_info 1  
  [Mkvar "count" KindInt]  
  (GAnd (GGt (TVar "count") (TIntLit 0))  
(GLE (TVar "count") (TIntLit 5)))
```

The Engine That Makes This Tractable: Shallow-to-Deep Embedding Extraction



Users write :

```
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```

Meta-F*

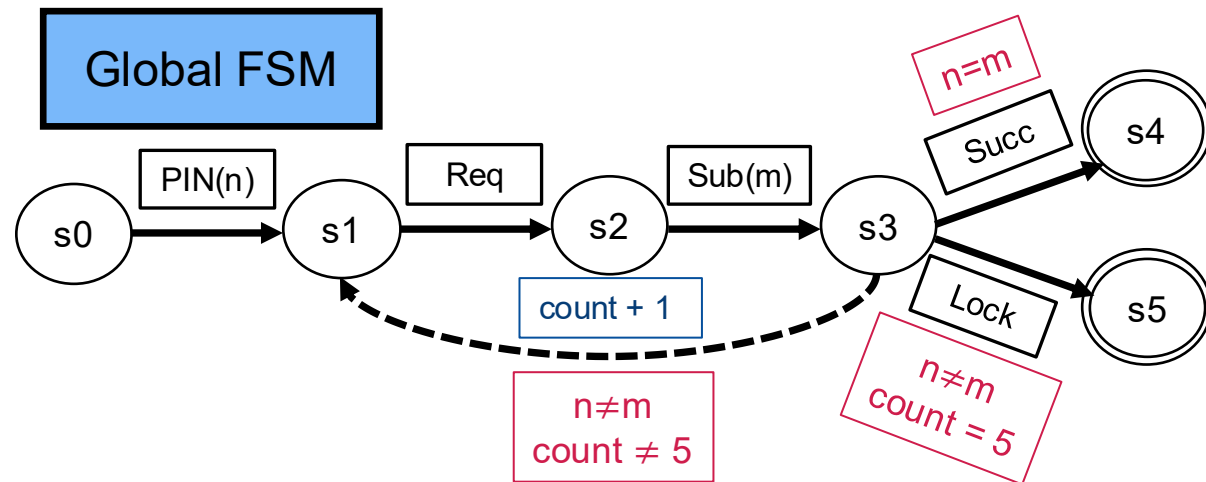


Users Prove:

```
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F*ACT Proves Application-Specific Safety Without State Explosion

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- "After 5 tries with wrong input, the account must be locked"

Operational Semantics

State + Command $\rightarrow$ State

Server $\rightarrow$ **Auth** : $\text{PIN}(\text{expected_code} : \mathbb{Z} \{ \text{expected_code} \geq 0 \wedge \text{expected_code} \leq 999999 \})$

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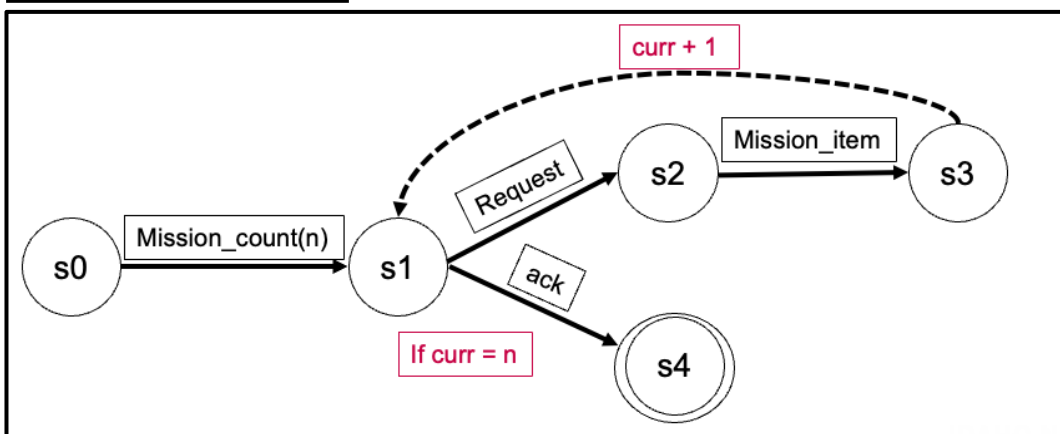
Auth $\rightarrow$ **User** : $\text{RequestAuth}(_ : \text{unit})$

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F*ACT Proves Application-Specific Safety Without State Explosion

Model Checking



- Automated
- Counterexample generation
- State explosion

Use it when possible

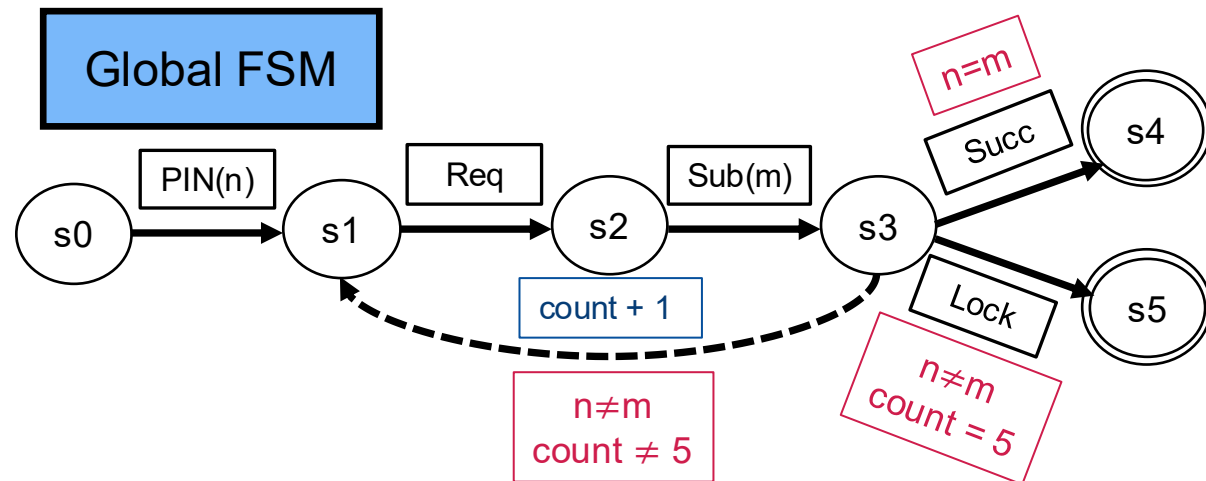
Theorem proving

- Proof scalability
- Handles infinite state protocols
- Complexity (interactive proofs)

Use it when model checking fails



Global FSM



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Operational Semantics

State + *Command* → *State*

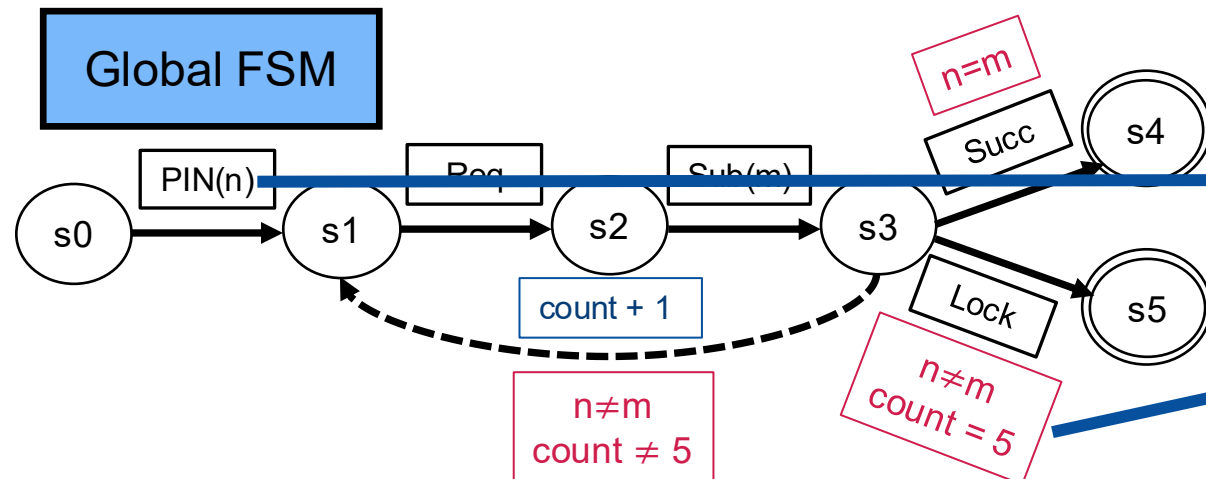
(n = 2; m = 3) + Succeed → **WRONG**

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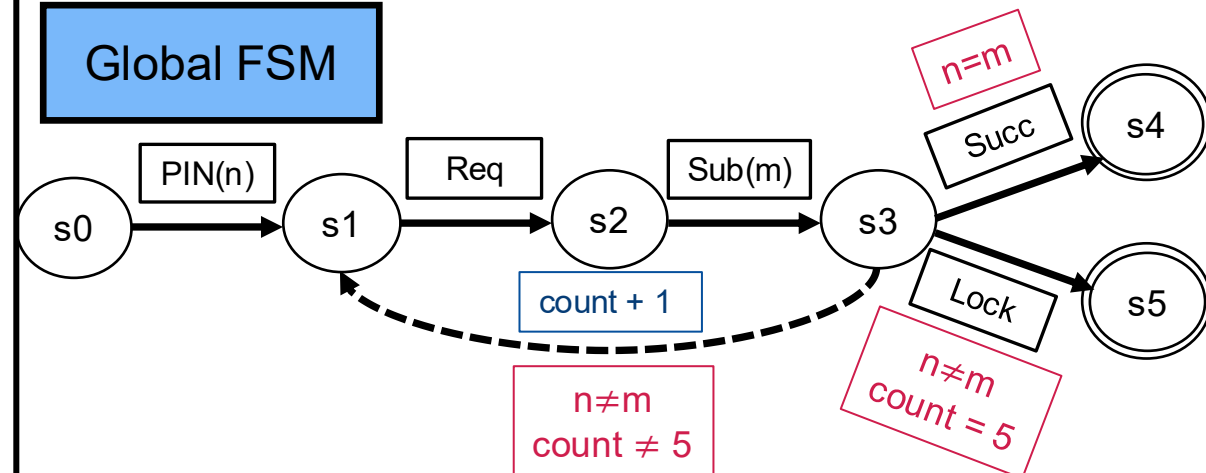
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